



Cambridge IGCSE™

CANDIDATE
NAME

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CENTRE
NUMBER

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CANDIDATE
NUMBER

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ADDITIONAL MATHEMATICS

0606/23

Paper 2

October/November 2020

2 hours

You must answer on the question paper.

No additional materials are needed.

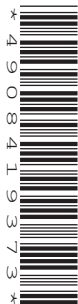
INSTRUCTIONS

- Answer **all** questions.
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs.
- Write your name, centre number and candidate number in the boxes at the top of the page.
- Write your answer to each question in the space provided.
- Do **not** use an erasable pen or correction fluid.
- Do **not** write on any bar codes.
- You should use a calculator where appropriate.
- You must show all necessary working clearly; no marks will be given for unsupported answers from a calculator.
- Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place for angles in degrees, unless a different level of accuracy is specified in the question.

INFORMATION

- The total mark for this paper is 80.
- The number of marks for each question or part question is shown in brackets [].

This document has **16** pages. Blank pages are indicated.



1 Solve $|3x-2|=4+x$.

[3]



2 Solve the simultaneous equations.



$$x^2 + 3xy = 4$$

$$2x + 5y = 4$$

[5]

3 Find the values of k for which the equation $x^2 + (k+9)x + 9 = 0$ has two distinct real roots. [4]



4 It is given that $y = \ln(1 + \sin x)$ for $0 < x < \pi$.



(a) Find $\frac{dy}{dx}$.

[2]

(b) Find the value of $\frac{dy}{dx}$ when $x = \frac{\pi}{6}$, giving your answer in the form $\frac{1}{\sqrt{a}}$, where a is an integer. [2]

(c) Find the values of x for which $\frac{dy}{dx} = \tan x$. [5]

5 Solve the following simultaneous equations.



$$3^x \times 9^{y-1} = 243$$

$$8 \times 2^{y-\frac{1}{2}} = \frac{2^{2x+1}}{4\sqrt{2}}$$

[5]

6 A 4-digit code is to be formed using 4 different numbers selected from 1, 2, 3, 4, 5, 6, 7, 8 and 9. Find how many different codes can be formed if



(a) there are no restrictions, [1]

(b) only prime numbers are used, [1]

(c) two even numbers are followed by two odd numbers, [2]

(d) the code forms an even number. [2]

7 A curve has equation $y = x \cos x$.



(a) Find $\frac{dy}{dx}$.

[2]

(b) Find the equation of the normal to the curve at the point where $x = \pi$, giving your answer in the form $y = mx + c$.

[4]

(c) Using your answer to **part (a)**, find the exact value of $\int_0^{\frac{\pi}{6}} x \sin x \, dx$.

[5]

8 DO NOT USE A CALCULATOR IN THIS QUESTION.



$$\log_2(y+1) = 3 - 2\log_2 x$$

$$\log_2(x+2) = 2 + \log_2 y$$

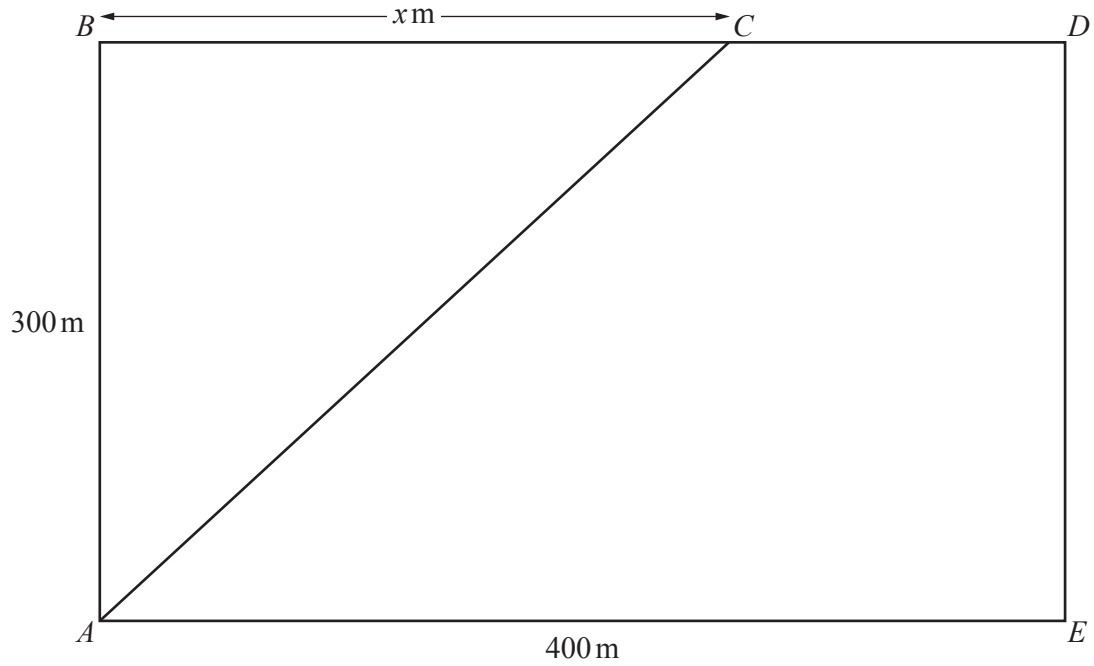
(a) Show that $x^3 + 6x^2 - 32 = 0$.

[4]

(b) Find the roots of $x^3 + 6x^2 - 32 = 0$.

[4]

(c) Give a reason why only one root is a valid solution of the logarithmic equations. Find the value of y corresponding to this root. [2]



The rectangle $ABCDE$ represents a ploughed field where $AB = 300$ m and $AE = 400$ m. Joseph needs to walk from A to D in the least possible time. He can walk at 0.9 ms^{-1} on the ploughed field and at 1.5 ms^{-1} on any part of the path BCD along the edge of the field. He walks from A to C and then from C to D . The distance $BC = x$ m.

- (a) Find, in terms of x , the total time, T s, Joseph takes for the journey. [3]

- (b) Given that x can vary, find the value of x for which T is a minimum and hence find the minimum value of T . [6]

- 10 (a) The sum of the first 4 terms of an arithmetic progression is 38 and the sum of the next 4 terms is 86. Find the first term and the common difference. [5]



- (b) The third term of a geometric progression is 12 and the sixth term is -96 . Find the sum of the first 10 terms of this progression. [6]

11 DO NOT USE A CALCULATOR IN THIS QUESTION.

Solve the quadratic equation $(\sqrt{7}-2)x^2 - 4x + (\sqrt{7}+2) = 0$, giving each of your answers in the form $a + b\sqrt{7}$, where a and b are constants. [7]