

Question	Answer	Marks	Partial Marks
1	$\frac{dy}{dx} = \cos x - e^{-x}$	<b>B2</b>	<b>B1</b> for $\cos x$ or $-e^{-x}$
	$\delta y = \text{their } \left. \frac{dy}{dx} \right _{x=\frac{\pi}{4}} \times h$	<b>M1</b>	
	0.251h	<b>A1</b>	
2	Squares: $(1-\sqrt{5})^2 = 1-\sqrt{5}-\sqrt{5}+5$	<b>B1</b>	or rationalises $\frac{10+2\sqrt{5}}{(1-\sqrt{5})^2} \times \frac{(1+\sqrt{5})^2}{(1+\sqrt{5})^2}$
	Rationalises, e.g. $\frac{10+2\sqrt{5}}{6-2\sqrt{5}} \times \frac{6+2\sqrt{5}}{6+2\sqrt{5}}$	<b>B1</b>	or squares $(1+\sqrt{5})^2 = 1+\sqrt{5}+\sqrt{5}+5$
	Multiplies out, e.g. $\frac{60+20\sqrt{5}+12\sqrt{5}+4(5)}{36-20}$	<b>M1</b>	Multiplies out $\left[ \frac{10+2\sqrt{5}}{(1-\sqrt{5})^2} \times \frac{6+2\sqrt{5}}{(1+\sqrt{5})^2} = \right]$ $\frac{60+20\sqrt{5}+12\sqrt{5}+4(5)}{(1-5)^2}$
	$5+2\sqrt{5}$	<b>A2</b>	A1 for $k+2\sqrt{5}$ or $5+k\sqrt{5}$
3	$x-3=k^2x^2+5kx+1$	<b>M1</b>	
	$k^2x^2+(5k-1)x+4=0$ soi	<b>A1</b>	
	$(5k-1)^2-4(k^2)(4)$	<b>M1</b>	
	$9k^2-10k+1=0$	<b>M1</b>	
	Critical values: $\frac{1}{9}$ and 1 soi	<b>A1</b>	
	$k < \frac{1}{9}$ or $k > 1$	<b>A1</b>	

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4	Factorised form: $(x+n)(x-n)(2x-1)$ oe	<b>B1</b>	
	Multiplies out correctly	<b>M1</b>	<b>FT</b> <i>their</i> factorised form provided of equivalent difficulty
	Correct expanded form in terms of $n$ : $2x^3 - x^2 - 2n^2x + n^2$	<b>A1</b>	
	Uses ( <i>their</i> $n^2$ ) = 4 in <i>their</i> expression	<b>M1</b>	
	$2x^3 - x^2 - 8x + 4$	<b>A1</b>	If <b>A0A0</b> then <b>SC1</b> for $(x+n)(x-n)(x-0.5)$ giving $n^2 = 8$ leading to $x^3 - \frac{1}{2}x^2 - 8x + 4$
			<b>Alternative method:</b> <b>B1</b> for factorised form: $(x+n)(x-n)(2x-1)$
			<b>M1</b> for <i>their</i> $n^2 = 4$
			<b>A1</b> for $n = 2$
			<b>M1</b> for multiplying out $(x+their 2)(x-their 2)(2x-1)$
			<b>A1</b> for $2x^3 - x^2 - 8x + 4$  If <b>A0A0</b> then <b>SC1</b> for $(x+n)(x-n)(x-0.5)$ giving $n^2 = 8$ leading to $x^3 - \frac{1}{2}x^2 - 8x + 4$
5(a)	Finds coordinates of mid-point $(8, -2)$	<b>B1</b>	
	$m_{AB} = \frac{3+7}{4-12} \left[ = -\frac{5}{4} \right]$ oe soi	<b>B1</b>	
	$m_L = \frac{-1}{-5/4}$ oe	<b>M1</b>	
	$y+2 = \frac{4}{5}(x-8)$ oe isw	<b>A1</b>	

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5(b)	$y - 12 = -\frac{5}{4}(x - 5)$	<b>B1</b>	
	Attempts to solve <i>their</i> equations	<b>M1</b>	
	(13, 2)	<b>A2</b>	<b>A1</b> for $x = 13$ or $y = 2$
6(a)	$\frac{dy}{dx} = \sec^2 2x$	<b>B1</b>	
	$\text{their} \frac{dy}{dx} \Big _{x=\frac{\pi}{8}} = \text{their} 2$	<b>B1</b>	<b>FT</b> <i>their</i> $\frac{dy}{dx}$
	$x = \frac{\pi}{8}, y = 4$	<b>B1</b>	
	$y - \text{their} 4 = (\text{their} 2) \left(x - \frac{\pi}{8}\right)$ oe	<b>M1</b>	
	$2x - y = \frac{\pi}{4} - 4$	<b>A1</b>	
6(b)	$\sqrt{\left(\frac{\pi}{8} - 2\right)^2 + \left(4 - \frac{\pi}{4}\right)^2}$ oe	<b>M1</b>	
	3.59 or 3.59[03...] rot to four or more figs	<b>A1</b>	
7(a)	$2\ln(5x + 2)$	<b>B2</b>	<b>B1</b> for $k\ln(5x + 2)$
	$2(\ln(22) - \ln(2))$ oe soi	<b>M1</b>	
	$2\ln 11$ or $\ln 121$ or $\ln 11^2$	<b>A1</b>	
7(b)	$\int e^{8x+4} dx$	<b>M1</b>	
	$\left[\frac{1}{8}e^{8x+4}\right]_0^{\ln 2}$ oe	<b>M1</b>	
	$\frac{1}{8}(e^{\ln 2^8} \times e^4 - e^4)$ oe	<b>M2</b>	<b>M1</b> for $\frac{1}{8}(e^{\ln 2^8 + 4} - e^4)$
	$\frac{255}{8}e^4$ or exact equivalent	<b>A1</b>	

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8(a)	$3(\operatorname{cosec}^2 x - 1) - 14 \operatorname{cosec} x - 2 [= 0]$	<b>M1</b>	
	$3 \operatorname{cosec}^2 x - 14 \operatorname{cosec} x - 5 = 0$	<b>A1</b>	
	$(\operatorname{cosec} x - 5)(3 \operatorname{cosec} x + 1)$	<b>M1</b>	
	$\sin x = \frac{1}{5}$ nfw	<b>A1</b>	
	11.5 and 168.5 nfw	<b>A1</b>	
8(b)	Correct use of $\sin^2 y + \cos^2 y = 1$	<b>B1</b>	
	Factorises using the difference of 2 squares	<b>B1</b>	
	Uses $\frac{1}{\cot y} = \tan y$ or $\cot y = \frac{\cos y}{\sin y}$ correctly	<b>B1</b>	
	Full and correct completion to given answer: $\tan y - 2 \cos y \sin y$	<b>B1</b>	
9(a)	$\frac{3^{10x}}{3^{3x-6}} [= 243]$ oe or $\log 9^{5x} - \log 27^{x-2} = \log 243$ oe	<b>B1</b>	
	$3^{7x+6} = 3^5$ soi oe or $5x(\log 9) - (x-2)\log 27 = \log 243$	<b>M1</b>	
	$x = -\frac{1}{7}$	<b>A1</b>	

Question	Answer	Marks	Partial Marks
9(b)	$\frac{1}{2} \log_a b - \frac{1}{2} = \frac{1}{\log_a b}$ or $\frac{\frac{1}{2}}{\log_b a} - \frac{1}{2} = \log_b a$	<b>B2</b>	<b>B1</b> for bringing down the power of $\frac{1}{2}$ e.g. $\frac{1}{2} \log_a b$ or for a change of base e.g. $\frac{1}{\log_a b}$
	Clears the fraction and rearranges $\frac{1}{2}(\log_a b)^2 - \frac{1}{2} \log_a b = 1$ oe $(\log_a b)^2 - \log_a b - 2 = 0$ oe or let $x = \log_a b$ $x^2 - x - 2 = 0$ oe or $\frac{1}{2} - \frac{1}{2} \log_b a = (\log_b a)^2$ $0 = 2(\log_b a)^2 + \log_b a - 1$ oe or let $y = \log_b a$ $2y^2 + y - 1 = 0$	<b>M1</b>	
	$(\log_a b - 2)(\log_a b + 1)$ oe or $(2 \log_b a - 1)(\log_b a + 1)$	<b>M1</b>	
	[ $\log_a b = 2$ , $\log_a b = -1$ or $\log_b a = \frac{1}{2}$ , $\log_b a = -1$ leading to ] $b = a^2$ , $b =$ oe	<b>A1</b>	
10(a)(i)	$4 \times (-0.5)^{19}$	<b>M1</b>	
	$-\frac{1}{131072}$ or $-7.63 \times 10^{-6}$ or $-7.62939... \times 10^{-6}$ rot to four or more figs	<b>A1</b>	
10(a)(ii)	Valid explanation e.g. the common ratio is between $-1$ and $1$	<b>B1</b>	
	$\frac{4}{1 - (-0.5)} = \frac{8}{3}$	<b>B1</b>	

Question	Answer	Marks	Partial Marks
10(b)(i)	$a + 9d = 15(a + d)$	<b>B1</b>	
	$\frac{6}{2}\{2a + 5d\} = 87$	<b>B1</b>	
	Solves <i>their</i> equations for $d$ e.g. $2\left(-\frac{3}{7}d\right) + 5d = 29$	<b>M1</b>	
	$d = 7$	<b>A1</b>	
10(b)(ii)	$a = -3$ soi	<b>B1</b>	
	$6990 = \text{their}(-3) + (n-1)(\text{their}7)$	<b>M1</b>	
	$n = 1000$	<b>A1</b>	
11(a)	[perimeter =] $\frac{4}{3}\pi r$ soi	<b>B2</b>	<b>B1</b> for angle $ACB = \frac{2}{3}\pi$
	$\left(\text{their} \frac{4}{3}\pi r\right) = 4\pi$ oe	<b>M1</b>	
	$r = 3$	<b>A1</b>	
11(b)	$\frac{1}{2} \times \text{their} 3^2 \times \text{their} \frac{2\pi}{3}$ oe	<b>M1</b>	
	$\frac{1}{2} \times \text{their} 3^2 \times \sin \text{their} \frac{2\pi}{3}$ oe	<b>M1</b>	
	For subtracting and doubling: $\text{their} 3^2 \times \text{their} \frac{2\pi}{3} -$ $\text{their} 3^2 \times \sin \text{their} \frac{2\pi}{3}$	<b>M1</b>	
	$6\pi - \frac{9}{2}\sqrt{3}$ or exact equivalent	<b>A1</b>	