

Question	Answer	Marks	Partial Marks
1	$x = 3$	B1	
	$2 - 3x = 4 + x$ oe	M1	
	$x = -0.5$ oe	A1	
2	$x^2 + 3x\left(\frac{4-2x}{5}\right) = 4$	M1	eliminate x or y
	$x^2 - 12x + 20 (=0)$	A1	3 terms on one side if eliminating y $5y^2 + 16y (=0)$ if eliminating x
	$(x-2)(x-10) (=0)$	M1	or $y(5y+16) (=0)$
	$x = 2$ or $x = 10$ nfw	A1	or correct pair
	$y = 0$ or $y = -\frac{16}{5}$ nfw	A1	
3	$(k+9)^2 - 4 \times 9 (>0)$	M1	use $b^2 - 4ac$
	$k^2 + 18k + 45 (>0)$	A1	
	$k = -15$ $k = -3$	A1	
	$k < -15$ or $k > -3$ no isw mark final answer	A1	not 'and' A0 if combined as one statement
4(a)	$\frac{dy}{dx} = \frac{1}{1 + \sin x}$	M1	
	$\times \cos x = \frac{\cos x}{1 + \sin x}$	A1	
4(b)	insert $\frac{\pi}{6}$ into <i>their</i> $\frac{dy}{dx}$	M1	
	$\frac{1}{\sqrt{3}}$	A1	not $\frac{\sqrt{3}}{3}$

Question	Answer	Marks	Partial Marks
4(c)	<i>their</i> $\frac{\cos x}{1 + \sin x} = \frac{\sin x}{\cos x}$	M1	replace $\tan x$ with $\frac{\sin x}{\cos x}$
	use $\cos^2 x = 1 - \sin^2 x$ ($2\sin^2 x + \sin x - 1 = 0$)	M1	earned when equation reduced to a quadratic in $\sin x$
	$(2\sin x - 1)(\sin x + 1) = 0$	M1	solve three term quadratic in $\sin x$
	$x = \frac{\pi}{6}$	A1	or 0.524 or better radians only if M0 M0 M0 and (a) and (b) correct, allow SC2 for $\tan x = \frac{1}{\sqrt{3}}, x = \frac{\pi}{6}$
	$x = \frac{5\pi}{6}$	A1	or 2.62 or better radians only A0 if extra solution(s) in range
5	express an equation correctly in powers of 3 or powers of 2	M1	
	$x + 2y - 2 = 5$ oe $(x + 2y = 7)$	A1	accept unsimplified
	$2x + 1 - 2.5 = 3 + y - 0.5$ oe $(2x - y = 4)$	A1	accept unsimplified
	solve correct equations for x or y	M1	
	$x = 3$ and $y = 2$	A1	
6(a)	3024	B1	
6(b)	24	B1	
6(c)	${}^4P_2 \times {}^5P_2$	M1	$4 \times 3 \times 5 \times 4$
	240 no isw	A1	
6(d)	${}^4P_1 \times {}^8P_3$	M1	$4 \times 8 \times 7 \times 6$
	1344 no isw	A1	
7(a)	$-x \sin x + \cos x$ isw	B2	accept unsimplified if incorrect allow B1 for $\frac{d}{dx}(\cos x) = -\sin x$ clearly seen

Question	Answer	Marks	Partial Marks
7(b)	$x = \pi, y = -\pi$	B1	or -3.14 or better
	$x = \pi, \frac{dy}{dx} = -1$	B1	from correct $\frac{dy}{dx}$
	gradient of normal = 1	M1	use $m_1 m_2 = -1$ with <i>their</i> grad of tangent
	$y = x - 2\pi$ cso	A1	or $y = x - 6.28$ or better fully correct solution
7(c)	$\int \text{their}(a) = x \cos x$ $(\int -x \sin x + \cos x dx = x \cos x)$	M1	*
	$\int \cos x dx = \sin x$	B1	clearly seen anywhere
	$-x \cos x + \sin x$	A1	implies previous marks if (a) is correct
	insert $\frac{\pi}{6}$ into <i>their</i> integral	M1	* dep
	$\frac{1}{2} - \frac{\pi\sqrt{3}}{12}$	A1	reject decimals
8(a)	$x^2(y+1) = 8$ oe	B1	
	$x + 2 = 4y$ oe	B1	
	$x^2 \left(\frac{x+2}{4} + 1 \right) = 8$	M1	eliminate y from correct equations
	$x^3 + 6x^2 - 32 = 0$	A1	answer given
8(b)	$x = 2$ or $x = -4$ seen or $(x-2)$ or $(x+4)$ seen	B1	
	find quadratic factor	M1	x^2 and 16 or long division to $x^2 + kx$ or x^2 and -8 or long division to $x^2 + kx$ not from expanding two linear factors
	$(x^2 + 8x + 16)$ or $(x^2 + 2x - 8)$	A1	
	$(x-2)(x+4)^2$ and $x = 2, -4, -4$	A1	answer only without working earns B1 above only

Question	Answer	Marks	Partial Marks
8(c)	no real value for $\log_2(-4)$ or $\log_2(-4+2)$	B1	must identify specific term in one of original equations and use $x = -4$
	$y=1$	B1	
9(a)	$(AC =) \sqrt{300^2 + x^2}$ seen isw	B1	
	time for $AC = \frac{\sqrt{300^2 + x^2}}{0.9}$ oe or time for $CD = \frac{400-x}{1.5}$ oe	M1	using clearly indicated value for <i>their</i> AC or <i>their</i> CD
	$T = \frac{\sqrt{300^2 + x^2}}{0.9} + \frac{400-x}{1.5}$ oe seen isw	A1	
9(b)	$\frac{dT}{dx} = \frac{1}{2} \frac{(300^2 + x^2)^{-\frac{1}{2}}}{0.9} \times 2x - \frac{2}{3}$ oe	B2	accept unsimplified; if incorrect allow B1 for correct differentiation of $(300^2 + x^2)^{\pm\frac{1}{2}}$
	set <i>their</i> $\frac{dT}{dx} = 0$	M1	$\frac{dT}{dx}$ must be a function of x
	$25x^2 = 9(300^2 + x^2)$ oe	A1	equation in x^2 with square root removed
	$x = 225$ (m)	A1	
	$T = 533$ (s) or $1600/3$ (exact value)	A1	or 8 min 53 s
10(a)	use S_4 or S_8	M1	
	$S_4 = \frac{4}{2}[2a + 3d] = 38$ ($2a + 3d = 19$)	A1	accept unsimplified
	$S_8 = \frac{8}{2}[2a + 7d] = 38 + 86$ ($2a + 7d = 31$) or $S_8 - S_4 = \frac{8}{2}[2a + 7d] - \frac{4}{2}[2a + 3d] = 86$ ($4a + 22d = 86$)	A1	accept unsimplified
	solve correct equations for a or d	M1	
	$a = 5$ and $d = 3$	A1	

Question	Answer	Marks	Partial Marks
10(b)	$ar^2 = 12$ soi	B1	
	$ar^5 = -96$ soi	B1	
	solve correct equations for a or r	M1	
	$r = -2$ and $a = 3$	A1	
	insert <i>their</i> a and r into S_{10} $\left(S_{10} = \frac{3(1 - (-2)^{10})}{1 - (-2)} \right)$	M1	
	-1023	A1	
11	$(\sqrt{7} - 2)(\sqrt{7} + 2) = 3$ soi	B1	seen anywhere
	use quadratic formula to solve for x	M1	
	$x = \frac{4 \pm \sqrt{16 - 4(\sqrt{7} - 2)(\sqrt{7} + 2)}}{2(\sqrt{7} - 2)}$	A1	
	$x = \frac{4 \pm 2}{2(\sqrt{7} - 2)}$	A1	or $4 \pm \sqrt{4}$ in numerator
	rationalise one of <i>their</i> solutions e.g. $\frac{4 + 2}{2(\sqrt{7} - 2)} \times \frac{(\sqrt{7} + 2)}{(\sqrt{7} + 2)}$	B1	full rationalisation statement must be shown
	$x = 2 + \sqrt{7}$ nfw	A1	
	$x = \frac{2}{3} + \frac{1}{3}\sqrt{7}$ nfw	A1	accept $\frac{2 + \sqrt{7}}{3}$