

Question	Answer	Marks	Partial Marks
1	$x^2 - 18x + 45 (= 0)$	B1	Expand and simplify to three terms.
	$(x - 15)(x - 3)(= 0)$ or $x = \frac{18 \pm \sqrt{18^2 - 4 \times 45}}{2}$ or $(x - 9)^2 = -45 + 81$	M1	Factorise or use formula on <i>their</i> 3 term quadratic or complete the square
	$x = 15$ and $x = 3$	A1	
	$x < 3$ or $x > 15$ or $(-\infty, 3) \cup (15, \infty)$	A1	oe Do not accept 'and'. Do not accept $3 > x > 15$. Mark final answer.
2	$\frac{2^{(2x+2)}}{2^{(x-1)}} = 2^{\frac{5x}{3}} \times 2^1$	M1	Convert all to powers of 2 – allow one error.
	$2^{(x+3)} = 2^{\left(\frac{5x}{3}+1\right)}$	M1	Use $\frac{2^x}{2^y}$ and $2^{(x-y)}$ correctly on <i>their</i> expression. Allow one arithmetic slip.
	$x + 3 = \frac{5x}{3} + 1$	M1	Dep on previous M1. Forms linear equation using <i>their</i> powers correctly.
	$x = 3$	A1	
3(a)	Gradient of line $\frac{3-1}{4-12} = \left(-\frac{1}{4}\right)$	B1	
	Gradient of perpendicular = 4	M1	$\frac{-1}{\text{their grad line}}$
	Mid-point is (8, 2)	B1	
	Equation: $\frac{y-2}{x-8} = 4$	M1	Using <i>their</i> perpendicular gradient and mid-point
	$y = 4x - 30$	A1	
3(b)	$x = 0 \rightarrow (y) = -30$	B1	FT equation must have 3 terms
	$y = 0 \rightarrow (x) = 7.5$	B1	FT equation must have 3 terms
	$AB = \sqrt{30^2 + 7.5^2} = 30.9$ or better	B1	nfww Accept exact answer of $\frac{15\sqrt{17}}{2}$

Question	Answer	Marks	Partial Marks
4	$x + y = 9$	B1	
	$(x + 1)^2 = y + 2$	B1	
	$x + (x + 1)^2 - 2 = 9$ or $(10 - y)^2 = y + 2$	M1	Replace y or x . Allow unsimplified using <i>their</i> three term expressions both containing x and y terms. Condone one sign or arithmetic error. Result must be a quadratic function.
	$x^2 + 3x - 10 (= 0)$ or $y^2 - 21y + 98 (= 0)$	A1	Correct 3 term quadratic
	$x = -5$ and $x = 2$ or $y = 7$ and $y = 14$ or $(x + 5)(x - 2)$ or $(y - 7)(y - 14)$	M1	Dep on correct method to solve their quadratic
	$x = 2$ and $y = 7$ only	A1	Reject $x = -5, y = 14$ as log -4 is not appropriate
5(a)	$x = 1 \rightarrow y = 8$	B1	
	$\frac{dy}{dx} = 3x^2 - 12x + 3$	M1	Attempt to differentiate. Powers reduced by 1 in all four terms.
	$x = 1 \rightarrow \frac{dy}{dx} = -6$	A1	
	$\frac{y-8}{x-1} = -6 \rightarrow y = -6x + 14$	A1	Either form. isw
5(b)	$x^3 - 6x^2 + 9x - 4 = 0$ $(x - 1)(x^2 - 5x + 4) = 0$ or $(x - 4)(x^2 - 2x + 1) = 0$	2	M1 for equating <i>their</i> tangent to curve and simplifying to 4 term cubic. M1Dep for finding a factor or stating that $(x - 1)$ is a factor or makes at least 3 attempts to find a factor.
	$(x - 1)(x - 1)(x - 4) = 0$	2	A1 for $(x - 1)$ or $x = 1$ can be implied. nfw A1 for $(x - 4)$ or $x = 4$ not repeated. nfw
	$x = 4 \rightarrow y = -10$ only	A1	nfw

Question	Answer	Marks	Partial Marks
6	$\frac{(x+1)^2}{x^2} = \frac{x^2 + 2x + 1}{x^2} = 1 + \frac{2}{x} + \frac{1}{x^2}$	2	B1 for expanding numerator seen anywhere. M1 for attempt to divide <i>their</i> three term numerator by x^2 .
	$\int 1 + \frac{2}{x} + \frac{1}{x^2} dx = x + 2 \ln x - \frac{1}{x} + (c)$	2	A2/1/0 minus 1 each error or omission.
	$\left[4 - 2 \ln 4 - \frac{1}{4} \right] - \left[2 + 2 \ln 2 - \frac{1}{2} \right]$	M1	Dep insert 4 and 2 into <i>their</i> three or two term integrand and subtract correctly.
	$= \frac{9}{4} + 2 \ln 2$	A1	oe must be exact two terms. isw
7 (a)	$a = 3 \quad r = \frac{2.4}{3} = 0.8$	B1	
	$S_8 = \frac{3(1 - 0.8^8)}{(1 - 0.8)}$	M1	Inserts <i>their</i> a and r into S_8
	$= 12.48$ awrt or 12.5	A1	
7(b)	$S_\infty = \frac{3}{(1 - 0.8)} = 15$	B1	
7(c)	$S_n = 15(1 - 0.8^n) > 0.95 \times 15$	M1	<i>their</i> correctly produced $S_n > 0.95S_\infty$
	$0.8^n < 0.05$	A1	oe
	$n < \frac{\log 0.05}{\log 0.8}$ or $n < \log_{0.8} 0.05$	M1	Dep takes logs correctly of <i>their</i> expression with power of n .
	$n = 14$	A1	nfww
8(a)	$\frac{1}{2}(2\sqrt{3} + 1) AC \sin 30^\circ = \frac{11}{2}$	M1	Correct use of area of a triangle
	$(2\sqrt{3} + 1) AC = 22$	A1	oe
	$AC = \frac{22}{(2\sqrt{3} + 1)} \times \frac{(2\sqrt{3} - 1)}{(2\sqrt{3} - 1)}$	M1	Multiply by <i>their</i> $(2\sqrt{3} + 1)$
	$AC = 4\sqrt{3} - 2$	A1	

Question	Answer	Marks	Partial Marks
8(b)	$BC^2 = (2\sqrt{3} + 1)^2 + (4\sqrt{3} - 2) - 2(2\sqrt{3} + 1)(4\sqrt{3} - 2)\cos 30$	M1	Correct use of cosine rule with <i>their AC</i> .
	$BC^2 = [13 + 4\sqrt{3}] + [52 - 16\sqrt{3}] + [-22\sqrt{3}]$	A2	A1 for one correct expanded bracket A1 for the other two correct expanded brackets
	$BC^2 = 65 - 34\sqrt{3}$	A1	
9(a)	$2\mathbf{b} + \mathbf{a}$	B1	
9(b)	$2\mathbf{a} - 2\mathbf{b}$	B1	
9(c)	$2\mathbf{b} + \mathbf{a} + \mu(2\mathbf{a} - 2\mathbf{b})$	B1	FT on <i>their</i> \overline{OQ} and \overline{QR} isw
9(d)	$\lambda(3\mathbf{a} + \mathbf{b})$	B1	$\lambda 3\mathbf{a} + \mathbf{b}$ is B0
9(e)	$3\lambda = 1 + 2\mu$ $\lambda = 2 - 2\mu$ $\lambda = \frac{3}{4}, \mu = \frac{5}{8}$	3	M1 for forming two simultaneous equations equating correct terms. Each equation must have 3 terms. M1Dep for attempting to solve by removing μ or λ to $\lambda =$ or $\mu =$ A1 for both
9(f)	$\frac{QX}{XS} = \frac{5}{3}$	B1	FT Must be positive from $\mu < 1$
9(g)	$\frac{OR}{OX} = \frac{4}{3}$	B1	FT Must be positive from $\lambda < 1$
10(a)	$P + Q = 500$ and $P + Qe^2 = 600$	B1	
	$Q = \frac{100}{(e^2 - 1)} = 15.7$ or 15.6	2	M1 for attempt to solve by removing P from two equations both containing 3 terms A1 awrt
	$P = 484$ or 485	A1	awrt
10(b)	$B = 484.3 + 15.65e^4 = 1338$	B1	Integer value rounded down from 1338... if seen.

Question	Answer	Marks	Partial Marks
10(c)	$e^{2t} = \frac{1000000 - 484.3}{15.65}$	M1	Make e^{2t} the subject
	$2t = \ln\left(\frac{1000000 - 484.3}{15.65}\right)$	M1	Take logs correctly where $e^{2t} > 0$ or $e^n > 0$
	$[t = 5.5(3) \text{ or } t = 5.5\dots] \rightarrow 6^{\text{th}} \text{ week.}$	A1	nfww
11(a)	$\text{LHS} = \frac{\sin x \times \frac{\sin x}{\cos x}}{1 - \cos x}$	M1	Uses $\tan x = \frac{\sin x}{\cos x}$
	$= \frac{1 - \cos^2 x}{\cos x(1 - \cos x)}$	M1	Dep Uses $\sin^2 x = 1 - \cos^2 x$ to eliminate $\sin x$
	$\frac{(1 - \cos x)(1 + \cos x)}{\cos x(1 - \cos x)} = \frac{1 + \cos x}{\cos x} = \sec x + 1$	2	M1Dep Factorise correctly and cancel correctly. A1 Uses $\frac{1}{\cos x} = \sec x$
11(b)	$5 \frac{\sin x}{\cos x} - 3 \frac{\cos x}{\sin x} = \frac{2}{\cos x}$	B1	Change $\tan x$, $\cot x$ and $\sec x$ into $\sin x$ and $\cos x$ correctly.
	$5\sin^2 x - 3(1 - \sin^2 x) = 2\sin x$	M1	Multiply correctly by $\sin x \cos x$ and use $\cos^2 x + \sin^2 x = 1$
	$8\sin^2 x - 2\sin x - 3 = 0$	A1	Three term quadratic.
	$(2\sin x + 1)(4\sin x - 3) = 0$	M1	Factorise or use formula on <i>their</i> quadratic
	$\sin x = -\frac{1}{2} \rightarrow x = 210^\circ, 330^\circ$	A1	
	$\sin x = \frac{3}{4} \rightarrow x = 48.6^\circ, 131.4^\circ$	A1	