

Question	Answer	Marks	Guidance
1(a)	$-3 < x < 1 \quad x > 5$	<b>B1</b>	
1(b)	$-\frac{1}{3}(x+3)(x-1)(x-5)$	<b>3</b>	<b>B1</b> for a negative cubic function <b>B1</b> for a cubic function multiplied by $\frac{1}{3}$ <b>B1</b> for $(x+3)(x-1)(x-5)$
2(a)	$a = \frac{10}{3}$ or $3\frac{1}{3}$	<b>B1</b>	
	$b = \frac{7}{3}$ or $2\frac{1}{3}$	<b>B1</b>	
	$c = \frac{9}{2}$ or $4\frac{1}{2}$ or 4.5	<b>B1</b>	
2(b)	$10(2^p)^2 - 17(2^p) + 3 = 0$ $(5(2^p) - 1)(2(2^p) - 3) = 0$ $2^p = \frac{1}{5}, 2^p = \frac{3}{2}$	<b>M1</b>	For recognition of a quadratic in $2^p$ , attempt to factorise and solve for $2^p$
	$p = \frac{\ln \frac{1}{5}}{\ln 2}$ or $p = \frac{\ln 1.5}{\ln 2}$ oe	<b>M1</b>	For correct attempt to deal with $2^p = k$
	-2.32	<b>A1</b>	
	0.585	<b>A1</b>	
3(a)	$\lg \frac{1000a^2}{b^4}$	<b>4</b>	<b>B1</b> for $3 = \lg 1000$
			<b>B1</b> for use of power rule once
			<b>B1</b> for use of addition or subtraction rule once
			<b>B1</b> All correct

Question	Answer	Marks	Guidance
3(b)	<b>Either</b> $3\log_a 4 = \frac{3}{\log_4 a}$	<b>B1</b>	
	$2(\log_4 a)^2 - 7\log_4 a + 3 = 0$ $(2\log_4 a - 1)(\log_4 a - 3) = 0$ $\log_4 a = \frac{1}{2}$ or $\log_4 a = 3$	<b>M1</b>	For obtaining a quadratic equation and solution
	$a = 4^{\frac{1}{2}}$ or $a = 4^3$	<b>M1</b>	<b>Dep</b> For dealing with the logarithm correctly once, may be implied by a correct solution
	64	<b>A1</b>	
	2	<b>A1</b>	
	<b>Or</b> $2\log_4 a = \frac{2}{\log_a 4}$	<b>(B1)</b>	
	$3(\log_a 4)^2 - 7\log_a 4 + 2 = 0$ $(3\log_a 4 - 1)(\log_a 4 - 2) = 0$ $\log_a 4 = \frac{1}{3}$ or $\log_a 4 = 2$	<b>(M1)</b>	For obtaining a quadratic equation and solution
	$a^{\frac{1}{3}} = 4$ or $a^2 = 4$	<b>(M1)</b>	<b>Dep</b> For dealing with the logarithm correctly once, may be implied by a correct solution
	64	<b>(A1)</b>	
	2	<b>(A1)</b>	
4	$\tan\left(2x + \frac{\pi}{3}\right) = \frac{1}{\sqrt{3}}$	<b>B1</b>	
	$x = -\frac{7\pi}{12}, -\frac{\pi}{12}, \frac{5\pi}{12}, \frac{11\pi}{12}$	<b>3</b>	<b>M1</b> for using correct order of operations <b>A1</b> for two correct solutions <b>A1</b> for two further correct solutions and no other solutions in range

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5	<b>Either</b> Maximum when $\sin \frac{x}{3} = 1$ or minimum when $\sin \frac{x}{3} = -1$	<b>M1</b>	For recognition that value of maximum or minimum is necessary
	$c = 9$	<b>A1</b>	
	$c = -1$	<b>A1</b>	
	<b>or</b> $\frac{dy}{dx} = \frac{5}{3} \cos \frac{x}{3}$ When $\frac{dy}{dx} = 0$ , $\sin \frac{x}{3} = +1$ or $-1$	<b>(M1)</b>	For differentiation, equating to zero to obtain values for $\sin \frac{x}{3}$
	$c = 9$	<b>(A1)</b>	
	$c = -1$	<b>(A1)</b>	
6(a)	$0 = -\frac{5}{4} + \frac{a}{4} + 5 + b$	<b>M1</b>	For use of the factor theorem
	$-24 = -10 + a + 10 + b$	<b>M1</b>	For use of the remainder theorem
	$a + 4b = -15$ $a + b = -24$ leading to	<b>M1</b>	<b>Dep</b> on both previous <b>M</b> marks for solution of <i>their</i> equations without using a calculator
	$a = -27, b = 3$	<b>A1</b>	
6(b)	$(2x + 1)(5x^2 \dots\dots\dots + \textit{their } b)$	<b>M1</b>	Allow for observation or algebraic long division. <i>Their</i> $a$ and $b$ must be integers.
	$(2x + 1)(5x^2 - 16x + 3)$	<b>A1</b>	
	$(2x + 1)(5x - 1)(x - 3)$	<b>2</b>	<b>M1</b> for attempt to factorise <i>their</i> 3-term quadratic <b>A1</b> all correct from fully correct working
6(c)	3	<b>B1</b>	<b>FT</b> on <i>their</i> (integer) $b$
7(a)(i)	<b>b – a</b>	<b>B1</b>	
7(a)(ii)	<b>c – b</b>	<b>B1</b>	

Question	Answer	Marks	Guidance
7(a)(iii)	$n\overline{AB} = m\overline{BC}$	<b>M1</b>	For substitution of <i>their</i> (i) and (ii) into $n\overline{AB} = m\overline{BC}$
	$na + mc = (m + n)b$	<b>A1</b>	For correct manipulation to obtain the <b>given answer</b>
7(b)	$2\lambda - 4\mu + 4 = 4\lambda + 4$ or $\lambda + 7\mu - 7 = -2\lambda - 2$	<b>M1</b>	For equating like components at least once, allow unsimplified
		<b>M1</b>	<b>Dep</b> for solving <i>their</i> equations to obtain both $\lambda$ and $\mu$
	$\mu = 5$	<b>A1</b>	
	$\lambda = -10$	<b>A1</b>	
8(a)	<b>Either</b> Starting with a 6: 120 ways	<b>B1</b>	May be implied by final answer
	Starting with 5, 7 or 9: 540 ways	<b>B1</b>	May be implied by final answer
	Total 660	<b>B1</b>	
	<b>Or Alternative 1</b> Ending with a 6: 180 ways	<b>(B1)</b>	May be implied by final answer
	Ending with 0 or 4: 480ways	<b>(B1)</b>	May be implied by final answer
	Total 660	<b>(B1)</b>	
	<b>Or Alternative 2</b> 11 ways of obtaining even 5-digit numbers which start with 5, 6, 7, 9	<b>(B1)</b>	For $11 \times k$ May be implied by final answer
	${}^5P_3$ ways of arranging remaining 3 digits: 60	<b>(B1)</b>	For $m \times 60$ where $m$ is from an attempt to list all cases for first and last digits May be implied by final answer
	$11 \times 60 = 660$	<b>(B1)</b>	
	<b>Or Alternative 3</b> Total arrangements ${}^7P_5$ minus (all odds + evens starting with 1 + evens starting with 0 or 4) $= 2520 - (1440 + 180 + 240)$	<b>(B2)</b>	For $2520 - (1440 + 180 + 240)$
660	<b>(B1)</b>		

Question	Answer	Marks	Guidance
8(b)	$\frac{n!}{(n-4)!4!} = \frac{6n!}{(n-2)!2!}$	<b>B1</b>	
	$(n-2)(n-3) = 72$	<b>2</b>	<b>B1</b> for $(n-2)(n-3)$
			<b>B1</b> for 72
	$n = 11$ only	<b>2</b>	<b>M1</b> for correct attempt to form and solve a quadratic equation <b>A1</b> for $n = 11$ only
9(a)	$AOD = 2 \times \tan^{-1}\left(\frac{2}{3}\right)$	<b>M1</b>	For correct method to find $AOD$
	$AOD = 1.1760\dots$ $AOD = 1.176$ [to 3dp]	<b>A1</b>	Need to see 4 dp or more to justify 3 dp answer
9(b)	Major arc $MN = (2\pi - 1.176)12$	<b>B1</b>	
	$ND$ or $MA = 12 - \sqrt{13}$	<b>B1</b>	
	Perimeter = major arc $MN + MA + ND + 16$ oe	<b>B1</b>	For <i>their</i> values in a correct plan, may be implied by a correct answer
	Perimeter = 94.1	<b>B1</b>	
9(c)	Minor sector area = $\frac{1}{2} \times 1.176 \times 12^2$ <b>or</b> Major sector area = $\frac{1}{2} \times (2\pi - 1.176) \times 12^2$	<b>B1</b>	
	Area = major sector area – remainder of rectangle or Area = area of circle – minor sector area – remainder of rectangle or Area = circle – rectangle – minor sector + triangle $AOD$	<b>B1</b>	For <i>their</i> values in a correct plan, may be implied by a correct answer
	Area = 350	<b>B1</b>	Allow greater accuracy
10(a)	At $A$ $y = 4$	<b>B1</b>	
	At $B$ $y = \frac{13}{16}$ or 0.8125	<b>B1</b>	

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10(b)	<b>Either</b> Area of trapezium = $\frac{231}{32}$	<b>B1</b>	Allow unsimplified
	$\int_{-1}^2 \frac{1}{(x+2)^2} + \frac{3}{x+2} dx$ $= \left[ -\frac{1}{x+2} + 3\ln(x+2) \right]_{-1}^2$	<b>2</b>	<b>B1</b> for $-\frac{1}{x+2}$ <b>B1</b> for $3\ln(x+2)$
	$\left[ \left( -\frac{1}{4} + 3\ln 4 \right) - (-1) \right]$	<b>M1</b>	For correct use of limits in <i>their</i> integral, but must have at least one of the two preceding <b>B</b> marks
	Area = $\frac{207}{32} - \ln 64$	<b>2</b>	<b>A1</b> for $\frac{207}{32}$ <b>A1</b> for $-\ln 64$
	<b>Or</b> $\int_{-1}^2 -\frac{17}{16}x + \frac{47}{16} - \frac{1}{(x+2)^2} - \frac{3}{x+2} dx$ $\left[ -\frac{17}{32}x^2 + \frac{47}{16}x + \frac{1}{x+2} - 3\ln(x+2) \right]_{-1}^2$	<b>(3)</b>	<b>B1</b> for $-\frac{17}{32}x^2 + \frac{47}{16}x$ <b>B1</b> for $\int \frac{1}{(x+2)^2} dx = -\frac{1}{x+2}$ <b>B1</b> for $\int \frac{3}{x+2} dx = 3\ln(x+2)$
	$\left( -\frac{17}{8} + \frac{47}{8} + \frac{1}{4} - 3\ln 4 \right) - \left( -\frac{17}{32} - \frac{47}{16} + 1 \right)$	<b>(M1)</b>	For correct use of limits in <i>their</i> integral, but must have at least one of the two preceding <b>B</b> marks
	Area = $\frac{207}{32} - \ln 64$	<b>(2)</b>	<b>A1</b> for $\frac{207}{32}$ <b>A1</b> for $-\ln 64$
11(a)(i)	0	<b>B1</b>	
11(a)(ii)	-3	<b>B1</b>	
11(a)(iii)	$\left( \frac{1}{2}(25+15) \times 30 \right) + \left( \frac{1}{2}(30+60) \times 10 \right) + \left( \frac{1}{2} \times 20 \times 60 \right)$	<b>M1</b>	For an unsimplified expression for the required area allowing at most one incorrect length
	Total distance = 1650	<b>A1</b>	
11(b)(i)	$v = 4 \cos \frac{5\pi}{3} - 4$ $= -2$	<b>M1</b>	
	Speed = 2	<b>A1</b>	

Question	Answer	Marks	Guidance
11(b)(ii)	$a = -12 \sin 3t$	<b>B1</b>	
	$\sin 3t = 0$ $3t = \pi$ Leading to	<b>M1</b>	For equating to zero and attempt to solve to obtain $t$ , allow if in degrees
	$t = \frac{\pi}{3}$	<b>A1</b>	
11(b)(iii)	$s = k \sin 3t - 4t (+c)$	<b>M1</b>	
	$s = \frac{4}{3} \sin 3t - 4t$	<b>A1</b>	