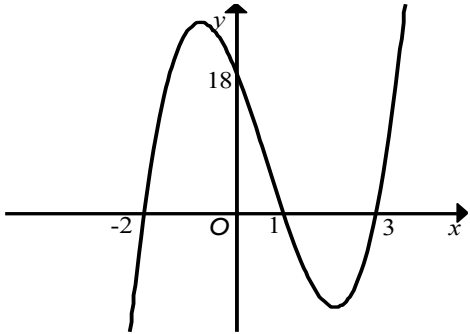
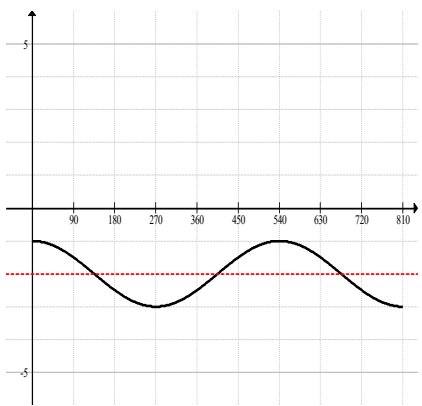


Question	Answer	Marks	Partial Marks
1	$1 + 4e^{2x} + 6e^{4x} + 4e^{6x} + e^{8x}$	<b>B2</b>	<p>mark final answer for <b>B2</b></p> <p><b>B1</b> for any 3 correct simplified terms in a sum or all 5 simplified terms listed but not summed or for a correct, simplified expansion that is not their final answer</p> <p>or</p> <p><b>M1</b> for a correct unsimplified expansion e.g.  <math>1 + 4e^{2x} + \frac{4 \times 3}{2}(e^{2x})^2 + \frac{4 \times 3 \times 2}{6}(e^{2x})^3 + (e^{2x})^4</math></p> <p>If 0 scored, <b>SC1</b> for a complete, correct, simplified expansion as final answer found by multiplying out the brackets</p>
2	<p>Correct graph and intercepts</p> 	<b>B3</b>	<p><b>B1</b> for correct shape; the ends must extend above and below the x-axis</p> <p><b>B1</b> for correct roots indicated; must have attempted a cubic shape</p> <p><b>B1</b> for correct y-intercept indicated; must have attempted a cubic shape</p>
3	<p>Uses <math>b^2 - 4ac</math> :</p> $6^2 - 4(2k - 1)(k + 1)$	<b>M1</b>	
	$-8k^2 - 4k + 40 * 0$ oe	<b>M1</b>	<p><b>dep</b> on first <b>M1</b></p> <p>where * is = or any inequality sign</p> <p>condone one sign or arithmetic slip in simplification</p>
	<p>Factorises or solves <i>their</i> 3-term quadratic expression or equation for CVs</p> <p>e.g. <math>(5 + 2k)(8 - 4k)</math> oe</p>	<b>M1</b>	
	Finds correct CVs: $-2.5$ oe, 2	<b>A1</b>	
	$-2.5 \leq k \leq 2$	<b>A1</b>	mark final answer

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4	$\frac{m}{27} - \frac{29}{9} + \frac{39}{3} + n = 0$ oe	<b>B1</b>	
	$m - 29 + 39 + n = 6$ oe	<b>B1</b>	
	Eliminates one unknown correctly for a pair of linear equations in $m$ and $n$ and solves for one unknown	<b>M1</b>	
	$m = 6, n = -10$	<b>A2</b>	<b>A1</b> for either
	[p(2) =] $48 - 116 + 78 - 10 = 0$ oe, nfw	<b>A1</b>	
5(a)	1	<b>B1</b>	
5(b)	$360 \div \frac{2}{3}$ oe	<b>M1</b>	
	540	<b>A1</b>	If 0 scored, <b>SC1</b> for $3\pi$
5(c)	Correct sketch for domain $0^\circ \leq x \leq 810^\circ$ 	<b>B2</b>	<b>B1</b> for correct cosine shape from $(0, -1)$ with amplitude 1 for $0^\circ \leq x \leq 810^\circ$  <b>B1</b> for attempt at correct cosine shape with period $540^\circ$ for $0^\circ \leq x \leq 810^\circ$  If 0 scored, <b>SC1</b> for a fully correct graph for $0^\circ \leq x \leq 540^\circ$  <b>Maximum of 1 mark if not fully correct.</b>
6(a)	$\sqrt{(11-5)^2 + (6-(-4))^2}$ oe	<b>M1</b>	
	11.7 or 11.66[19...] rot to 4 or more figs	<b>A1</b>	
6(b)(i)	[y = ] 1	<b>B1</b>	

Question	Answer	Marks	Partial Marks
6(b)(ii)	$m_{AC} = \frac{6-4}{11-5}$ or $\frac{10}{6}$ nfwwoe	<b>B1</b>	
	$m_{BD} = \frac{-1}{\text{their } \frac{10}{6}}$ oe	<b>M1</b>	
	$y - \text{their } 1 = -\frac{3}{5}(x-8)$ oe isw	<b>A1</b>	<b>FT</b> <i>their</i> 1 from (b)(i) and <i>their</i> perpendicular gradient
6(b)(iii)	$\begin{pmatrix} -5 \\ 3 \end{pmatrix}$ and $\begin{pmatrix} 5 \\ -3 \end{pmatrix}$	<b>B2</b>	<b>B1</b> for either If 0 scored, <b>SC1</b> for $-5\mathbf{i} + 3\mathbf{j}$ and $5\mathbf{i} - 3\mathbf{j}$
7(a)	[Arc length + 2 × tangent length] $18 \times \frac{7\pi}{9} + 2 \times 18 \times \tan \frac{7\pi}{18}$ oe	<b>M2</b>	<b>M1</b> for [Arc length] $18 \times \frac{7\pi}{9}$ oe or [Tangent length] $18 \times \tan \frac{7\pi}{18}$ oe or [Tangent length] $\frac{18}{\tan \frac{\pi}{9}}$ oe or [Tangent length] $\frac{18}{\sin \frac{\pi}{9}} \times \sin \frac{7\pi}{18}$ oe
	143 or 142.9 or awrt 142.9 (cm)	<b>A1</b>	
7(b)	[Area of kite – area of sector] $18 \times \text{their} \left( 18 \times \tan \frac{7\pi}{18} \right) - \frac{1}{2} \times 18^2 \times \frac{7\pi}{9}$ oe	<b>M2</b>	<b>FT</b> <i>their</i> <i>BC</i> or <i>CD</i> from (a) providing it is not 18 <b>M1</b> for [area of sector] $\frac{1}{2} \times 18^2 \times \frac{7\pi}{9}$ oe or [area of kite] $18 \times \text{their} \left( 18 \times \tan \frac{7\pi}{18} \right)$ oe or [area of kite] $18 \times \text{their} (18 \times \tan 70)$ oe
	494 or 494.3 or awrt 494.3 (cm <sup>2</sup> )	<b>A1</b>	

Question	Answer	Marks	Partial Marks
8(a)	Factorises or solves $3t^2 - 30t + 72 = 0$ or $t^2 - 10t + 24 = 0$	<b>M1</b>	
	$t = 4, t = 6$	<b>A1</b>	
	Integrates $v$ to find $F(t)$ : $\frac{3t^3}{3} - \frac{30t^2}{2} + 72t$	<b>M2</b>	<b>M1</b> for any two terms correct
	Correct substitution for $F(6) - F(4)$ or $F(4) - F(6)$	<b>M1</b>	<b>dep</b> on at least <b>M1</b> for integration <b>FT</b> <i>their</i> 4 and <i>their</i> 6 provided they are <b>both positive</b>
	4 (m)	<b>A1</b>	<b>dep</b> on all previous marks being awarded
8(b)	$[a =] 6t - 30$	<b>B1</b>	
	[When $t = 2$ : $a = 6(2) - 30 =$ $-18 \text{ (ms}^{-2}\text{) cao}$	<b>B1</b>	
9	Correctly eliminates $x$ or $y$ e.g. $4x^2 + 3x\left(-\frac{4}{x}\right) + \left(-\frac{4}{x}\right)^2 = 8$ oe or $4\left(-\frac{4}{y}\right)^2 + 3\left(-\frac{4}{y}\right)y + y^2 = 8$ oe	<b>M1</b>	
	Rearranges to a 3-term quadratic in $x^2$ or $y^2$ soi e.g. $4x^4 - 20x^2 + 16 = 0$ or $y^4 - 20y^2 + 64 = 0$	<b>A1</b>	
	Factorises or solves <i>their</i> 3-term quadratic in $x^2$ or $y^2$ soi : $(x^2 - 1)(x^2 - 4)$ or $(y^2 - 16)(y^2 - 4)$	<b>M1</b>	
	$x^2 = 1, x^2 = 4$ oe, nfww or $y^2 = 16, y^2 = 4$ oe, nfww	<b>A1</b>	
	$x = \pm 1, x = \pm 2$ $y = \mp 4, y = \mp 2$ oe, nfww	<b>A2</b>	<b>A1</b> for all 4 $x$ values or all 4 $y$ values
10(a)	$\frac{1}{3}e^{3x+3} + c$ or $\frac{1}{3}e^3 \times e^{3x} + c$ nfww	<b>B2</b>	<b>B1</b> for $ke^{3x+3}$ or $ke^3 \times e^{3x}$ where $k \neq \frac{1}{3}$ or 0

Question	Answer	Marks	Partial Marks
10(b)(i)	$\frac{d(\sin 4x)}{dx} = 4 \cos 4x$ soi	<b>B1</b>	
	Applies correct form of product rule: $4x \cos 4x + [1] \sin 4x$ isw	<b>B1</b>	FT <i>their</i> $4 \cos 4x$ if possible
10(b)(ii)	$\left[ \int (4x \cos 4x) dx = \right] x \sin 4x - \int \sin 4x dx$	<b>M1</b>	FT use of <i>their</i> $m x \cos 4x + n \sin 4x$ where $m$ and $n$ are constants
	$x \sin 4x + \frac{1}{4} \cos 4x [+c]$ soi	<b>A1</b>	
	$\frac{\pi}{3} \sin\left(4 \times \frac{\pi}{3}\right) + \frac{1}{4} \cos\left(4 \times \frac{\pi}{3}\right) -$ $\left[ \frac{\pi}{4} \sin\left(4 \times \frac{\pi}{4}\right) + \frac{1}{4} \cos\left(4 \times \frac{\pi}{4}\right) \right]$	<b>A1</b>	
	Correct completion to <b>given answer</b> $\frac{1}{8} - \frac{\pi\sqrt{3}}{6}$	<b>A1</b>	
11(a)	$500 = \frac{4}{6} \pi x^3 + \pi x^2 y$ oe	<b>M1</b>	
	$y = \frac{1}{\pi x^2} \left( 500 - \frac{4}{6} \pi x^3 \right)$ oe, isw	<b>A1</b>	if first <b>M0</b> , <b>SC1</b> for $y = \frac{1}{\pi x^2} \left( 500 - \frac{4}{6} \pi x^3 \right)$ oe seen
	$S = 2\pi x^2 + \pi x^2 + 2\pi x \left( \frac{500}{\pi x^2} - \frac{2}{3} x \right)$	<b>M1</b>	dep on first <b>M1</b>
	Correct completion to given answer: $S = \frac{5}{3} \pi x^2 + \frac{1000}{x}$	<b>A1</b>	
11(b)	Differentiates $S$ : $\frac{10}{3} \pi x - \frac{1000}{x^2}$ oe	<b>B2</b>	<b>B1</b> for each term
	$\frac{10}{3} \pi x - \frac{1000}{x^2} = 0$ and attempt to solve	<b>M1</b>	FT <i>their</i> $\frac{dS}{dx}$ providing at least <b>B1</b> awarded
	$x = \sqrt[3]{\frac{300}{\pi}}$ isw or 4.57[07...] nfw	<b>A1</b>	
12(a)(i)	$A(0,1)$ and $B(1,0)$	<b>B1</b>	

Question	Answer	Marks	Partial Marks
12(a)(ii)	$[y =] \frac{1}{2(2)+1}$ and $[y =] \frac{2-1}{5}$ <b>and</b> evaluates both expressions as $\frac{1}{5}$	<b>B2</b>	<b>B1</b> for $[y =] \frac{1}{2(2)+1}$ <b>and</b> $5y = 2 - 1$ oe
	Alternative 1  $[y =] \frac{1}{2(2)+1} = \frac{1}{5}$ or $[y =] \frac{2-1}{5} = \frac{1}{5}$ <b>and</b> solves $5 \times \frac{1}{5} = x - 1$ oe to get $x = 2$ or $\frac{1}{5} = \frac{1}{2x+1}$ oe to get $x = 2$	<b>(B2)</b>	<b>B1</b> for $\frac{1}{2(2)+1} = \frac{1}{5}$ and $5 \times \frac{1}{5} = x - 1$ oe or $\frac{2-1}{5} = \frac{1}{5}$ and $\frac{1}{5} = \frac{1}{2x+1}$ oe
	Alternative 2  $2x^2 - x - 6 = 0$ <b>and</b> solves or factorises to get $(2x + 3)(x - 2)$ and states $x = 2$ OR shows $2(2^2) - 2 - 6 = 0$ oe	<b>(B2)</b>	<b>B1</b> for $(2x + 1)(x - 1) = 5$ or $2x^2 - x - 6 = 0$
	Alternative 3  $(2x + 1)(x - 1) = 5$ oe <b>and</b> shows $(2 \times 2 + 1)(2 - 1) = 5$	<b>(B2)</b>	<b>B1</b> for $(2x + 1)(x - 1) = 5$
12(b)	$\frac{1}{2} \times 1 \times 0.2$ oe or $\frac{2^2}{5 \times 2} - \frac{2}{5} - \left( \frac{1^2}{5 \times 2} - \frac{1}{5} \right)$ oe	<b>B1</b>	
	$[F(x) =] \frac{1}{2} \ln(2x+1) [+c]$ oe or $\frac{1}{2} \ln(x+0.5) [+c]$ oe	<b>B2</b>	<b>B1</b> for $\frac{1}{2} \ln 2x+1$ or $\frac{1}{2} \ln x+0.5$ or $k \ln(2x+1)$ or $k \ln(x+0.5)$ , $k \neq 0.5$ or $0$
	$F(2) - F(0) - \text{their } 0.1$	<b>M1</b>	<b>FT</b> <i>their</i> $F(x)$ providing at least <b>B1</b> for integration of curve awarded
	$0.5 \ln 5 - 0.1$ or exact equivalent	<b>A1</b>	

Question	Answer	Marks	Partial Marks
13(a)	$[fg(x) =] \frac{2\left(\frac{1}{x}\right)^2 - 1}{3\left(\frac{1}{x}\right)} \text{ oe}$	<b>M1</b>	
	$[fg(x) =] \frac{2-x^2}{3x} \text{ or } \frac{2}{3x} - \frac{x}{3}$	<b>A1</b>	mark final answer
13(b)(i)	$f^{-1} > 0$	<b>B1</b>	
13(b)(ii)	$2x^2 - 3xy - 1 = 0$ or $2y^2 - 3xy - 1 = 0$	<b>B1</b>	
	Correctly applies quadratic formula: $[x =] \frac{-(-3y) \pm \sqrt{(-3y)^2 - 4(2)(-1)}}{2(2)} \text{ oe}$ or $[y =] \frac{-(-3x) \pm \sqrt{(-3x)^2 - 4(2)(-1)}}{2(2)} \text{ oe}$	<b>M1</b>	<b>FT</b> <i>their</i> $2x^2 - 3xy - 1 = 0$ or $2y^2 - 3xy - 1 = 0$ with at most one sign error in the equation
	Justifies the positive square root at some point	<b>B1</b>	
	$f^{-1}(x) = \frac{3x + \sqrt{9x^2 + 8}}{4} \text{ cao}$	<b>A1</b>	must be a function of $x$