

Question	Answer	Marks	Partial Marks
1	$x^2 + 3x - 10 - 3x - 6 * 0$ oe	M1	Condone one sign or arithmetic error * can be = or any inequality sign
	Critical Values: 4 and -4	A1	
	$x > 4$ or $x < -4$	A1	Mark final answer
2	Eliminate one unknown $x(11-3x)+x^2=15$	M1	
	$2x^2 - 11x + 15 [=0]$	A1	
	Factorises or solves <i>their</i> 3-term quadratic	M1	
	$x = \frac{5}{2}, y = \frac{7}{2}$ $x = 3, y = 2$	A2	A1 for $x = \frac{5}{2}, x = 3$ nfw or $y = \frac{7}{2}, y = 2$ nfw
3(a)	$\frac{d}{dx}(\sin 3x) = 3 \cos 3x$ soi	B1	
	Applies the correct form of the quotient rule	M1	
	$\frac{dy}{dx} = \frac{(x+1)(3 \cos 3x) - (2 + \sin 3x)[1]}{(x+1)^2}$	A1	FT <i>their</i> $\frac{d}{dx}(\sin 3x)$
	$\frac{dy}{dx} = \frac{\left(\frac{\pi}{6} + 1\right)\left(3 \cos \frac{3\pi}{6}\right) - \left(2 + \sin \frac{3\pi}{6}\right)[1]}{\left(\frac{\pi}{6} + 1\right)^2}$	M1	
	$\left[\frac{dy}{dx} = \right] \frac{-3}{\left(\frac{\pi}{6} + 1\right)^2}$	A1	not from wrong working

Question	Answer	Marks	Partial Marks
3(b)	[When $x = 0$] $y = 2$	B1	
	[When $x = 0$] $\frac{dy}{dx} = 1$	B1	FT <i>their</i> $\frac{dy}{dx}$
	$[m_{\perp} =] = -1$	M1	FT $\frac{-1}{\text{their}1}$
	$y - 2 = -x$ oe	A1	FT <i>their</i> m_{\perp}
4	$(\sqrt{5} - 2)a + (\sqrt{5} + 2)b = 1$ oe, soi	M1	
	$2b - 2a = 1$	A1	
	$a + b = 0$ or $a\sqrt{5} + b\sqrt{5} = 0$	A1	
	Solves <i>their</i> linear simultaneous equations in a and b as far as $a = \dots$ or $b = \dots$	M1	dep on previous M1
	$a = -\frac{1}{4}, b = \frac{1}{4}$	A1	
5(a)	$\frac{dy}{dx} = 6 \tan x \sec^2 x$	B2	B1 for $\frac{d}{dx}(\tan^2 x) = 2(\tan x)^1 \sec^2 x$
5(b)	$6 \tan x \sec^2 x - 3 \sec x \operatorname{cosec} x = 0$ $3 \sec x(2 \tan x \sec x - \operatorname{cosec} x) = 0$ oe	B1	NB division by $\sec x$ is B0
	$2 \tan^2 x = 1$ oe	B1	
	$\tan x = [\pm] \sqrt{\frac{1}{2}}$ or $[\pm] 0.707[1\dots]$	M1	FT $\tan^2 x = k$ where $k > 0$
	35.3 or 35.2643... rot to 2 or more dp 215.3 or 215.2643... rot to 2 or more dp 144.7 or 144.7356... rot to 2 or more dp 324.7 or 324.7356... rot to 2 or more dp	A2	no extras in range A1 for any two correct answers

Question	Answer	Marks	Partial Marks
6	$(m+1)x^2 + (8-m)x + 3 = 0$ oe, soi	B1	
	$(8-m)^2 - 4(m+1)(3)$	M1	
	$m^2 - 28m + 52$ [*0] oe	M1	dep on previous M1 ; condone one sign error where * is = or any inequality sign
	Factorises or solves <i>their</i> 3-term quadratic expression or equation for CVs	M1	dep on use of $b^2 - 4ac$
	Finds correct CVs: 2, 26	A1	
	$2 < m < 26$	A1	Mark final answer
7(a)	$\log 5^{x-2} = \log 3 + \log 2^{2x+3}$ soi	M1	
	$(x-2)\log 5 = \log 3 + (2x+3)\log 2$ oe	M1	dep on previous M1 ; Condone one sign or bracketing error
	$x = \frac{\log 3 + 3\log 2 + 2\log 5}{\log 5 - 2\log 2}$ soi	A1	
	$x = 28.7$	A1	
7(b)	$\log_3 \left(\frac{y^2 + 11}{9} \right) = \log_3 (y - 1)$ or $\log_3 \left(\frac{y^2 + 11}{y - 1} \right) = 2$ oe	B1	
	$\frac{y^2 + 11}{9} = y - 1$ or $\frac{y^2 + 11}{y - 1} = 9$ oe	M1	
	$y^2 - 9y + 20 = 0$	A1	
	Solves <i>their</i> 3-term quadratic	M1	dep on previous M1
	$y = 4, y = 5$	A1	
8(a)	252	B1	

Question	Answer	Marks	Partial Marks																								
8(b)	[2 men and 3 others =] 120 [3 men and 2 others =] 60 [4 men and 1 other =] 6	M2	M1 for any two correct																								
	186	A1																									
	Alternative method																										
	[0 men =] 6 [1 man and 4 others =] 60	(M1)																									
	(<i>their</i> 252) – (6 + 60)	(M1)																									
	186	(A1)																									
8(c)	<table border="1" style="display: inline-table; vertical-align: top;"> <thead> <tr> <th>M</th> <th>W</th> <th>C</th> <th></th> </tr> </thead> <tbody> <tr> <td>1</td> <td>3</td> <td>1</td> <td>32</td> </tr> <tr> <td>1</td> <td>2</td> <td>2</td> <td>24</td> </tr> <tr> <td>2</td> <td>2</td> <td>1</td> <td>72</td> </tr> <tr> <td>2</td> <td>1</td> <td>2</td> <td>24</td> </tr> <tr> <td>3</td> <td>1</td> <td>1</td> <td>32</td> </tr> </tbody> </table>	M	W	C		1	3	1	32	1	2	2	24	2	2	1	72	2	1	2	24	3	1	1	32	M2	for at least four out of five correct values soi or M1 for any two or three correct values soi
	M	W	C																								
	1	3	1	32																							
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	2	2	1	72																							
	2	1	2	24																							
3	1	1	32																								
184	A1																										
Alternative method																											
[0 men =] 6 [0 women] 6 [0 children] 56	(M1)																										
(<i>their</i> 252) – (6 + 6 + 56)	(M1)																										
184	(A1)																										
9(a)	$[fg(x) =] \frac{x^2 + 4}{x^2}$ oe, final answer	2	B1 for an attempt at the correct order of composition with at most one error																								
9(b)	Complete, correct method to find the inverse	M1																									
	$[g^{-1}(x) =] \sqrt{x-1}$ final answer	A1																									

Question	Answer	Marks	Partial Marks
9(c)	$x^3 - x^2 - 4 = 0$	M1	condone one sign or arithmetic error
	Shows $x - 2$ is a factor or shows that $x = 2$ is a solution	M1	
	Uses $x - 2$ is a factor to find $x^2 + x + 2$	B2	B1 for a quadratic factor with 2 terms correct
	Indicates that $x^2 + x + 2$ has no real roots and states $x = 2$ as the only solution	A1	dep on all previous marks awarded
10(a)	$\frac{dy}{dx} = -5x^{-2} + 2x - 1$ oe	M2	M1 for any two correct terms
	[When $x = 1$] $\frac{dy}{dx} = -4$ and $y = 5$	A1	
	$y - 5 = -4(x - 1)$ oe	M1	FT their $\frac{dy}{dx} \Big _{x=1}$ and y ; dep on at least M1
	$y = -4x + 9$	A1	FT
10(b)	$F(x) = 5 \ln x + \frac{x^3}{3} - \frac{x^2}{2} (+c)$	B2	B1 for $5 \ln x$ and one other term correct
	$F(3) - F(1)$	M1	dep on at least B1 for integration
	$5 \ln 3 + \frac{14}{3}$	A1	

Question	Answer	Marks	Partial Marks
11(a)	$l = \frac{4}{r}$	B1	
	$h^2 = l^2 - r^2$ or $l^2 = r^2 + h^2$	M1	
	$h^2 = \left(\frac{4}{r}\right)^2 - r^2$ or $\left(\frac{4}{r}\right)^2 = r^2 + h^2$ or $l^2 = \frac{16}{r^2}$ and $h^2 = l^2 - r^2$	M1	FT their l ; dep on previous M1
	Correct, convincing completion to $h^2 = \frac{16}{r^2} - r^2$	A1	
	Alternative method		
	$l = \sqrt{r^2 + h^2}$	(B1)	
	$\pi r \sqrt{r^2 + h^2} = 4\pi$	(M1)	
	$(\sqrt{r^2 + h^2})^2 = \left(\frac{4}{r}\right)^2$	(M1)	
	Correct, convincing completion to $h^2 = \frac{16}{r^2} - r^2$	(A1)	
11(b)	$\frac{\pi}{3} r^2 \sqrt{\frac{16}{r^2} - r^2}$	M1	
	$\frac{\pi}{3} \sqrt{r^4 \left(\frac{16}{r^2} - r^2\right)}$ and correct completion to $\frac{\pi}{3} \sqrt{16r^2 - r^6}$	A1	

Question	Answer	Marks	Partial Marks
11(c)	$\frac{dV}{dr} = \frac{\pi}{3} \left(\frac{1}{2} (16r^2 - r^6)^{-\frac{1}{2}} \right) (32r - 6r^5)$ oe	B3	B2 for $k(16r^2 - r^6)^{-\frac{1}{2}}(32r - 6r^5)$ where k is a constant and $k \neq 0$ or B1 for $k(16r^2 - r^6)^{-\frac{1}{2}} \times (f(r))$ where $f(r) \neq 32r - 6r^5$
	Equates <i>their</i> $\frac{dV}{dr}$ to 0 and solves as far as $r^4 = \dots$	M1	FT <i>their</i> $f(r) = ar + br^5$ for $a, b \neq 0$
	$r = 1.52$ or $1.519[67\dots]$ rot to 4 or more sf or $\frac{2}{\sqrt[4]{3}}$ oe	A1	