

Question	Answer	Marks	Partial Marks
1(a)	$w - 1 = \log_5 12$ or $w - 1 = \frac{\log 12}{\log 5}$	M1	
	$w = 2.54$ cao	A1	
1(b)	Rewrites in quadratic form e.g.: $y = x^{\frac{1}{3}} \quad y^2 - 5y + 6 = 0$ or $\left(x^{\frac{1}{3}}\right)^2 - 5x^{\frac{1}{3}} + 6 = 0$	M1	
	and factorises or solves e.g. : $(y - 2)(y - 3) = 0$	M1	Factorising <i>their</i> 3 term quadratic
	$x = 8$ and $x = 27$	A1	
2(a)	$\lg \frac{x^2}{3(x+6)}$ oe, nfw	B2	B1 for any two log laws applied correctly e.g. $\lg \frac{x^2}{x+6} - \lg 3$
2(b)	$\lg \frac{x^2}{3(x+6)} = \lg 1$ or $10^0 = \frac{x^2}{3(x+6)}$	B1	FT <i>their</i> $\lg \frac{x^2}{3(x+6)}$ providing a single logarithm
	$x^2 - 3x - 18 = 0$	B1	dep on B2 in part (a)
	Factorises or solves their 3-term quadratic	M1	
	$x = 6$ indicated as only solution	A1	dep on B2 in part (a)
3	Valid method to find m $m = \frac{8-1}{9-16} [= -1]$	M1	
	Valid method to find c e.g. $1 = \text{their}(-1) \times 16 + c$	M1	FT <i>their</i> m
	$\sqrt[3]{y} = \text{their}(-1)x^2 + \text{their}17$	A1	Equation with correct variables and $\sqrt[3]{y} =$
	$y = (-x^2 + 17)^3$ oe, isw	A1	

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4	$27m - 153 + 3n + 6 = 0$ or better	B1	
	$-m - 17 - n + 6 = -12$ or better	B1	
	Eliminates one unknown for a pair of linear equations in m and n and solves for one unknown	M1	
	$m = 6, n = -5$	A2	A1 for either
	-24 cao	A1	
5(a)(i)	$1 + 4nx + 8n(n - 1)x^2$	B2	B1 for any two correct terms or all 3 correct but listed not summed
5(a)(ii)	$8n(n - 1) - 16n$	M1	FT from (i) identifying correct terms and combining <i>their</i> coefficient of $x^2 - 4 \times$ <i>their</i> coefficient of x
	Solves or factorises <i>their</i> 3-term quadratic in n only	M1	Forms a 3-term quadratic = 0 and solves except allow ‘= a constant’ if they go on to complete to square
	$n = 29$ only	A1	
5(b)	${}^{10}C_2 \times \left(\frac{x}{2}\right)^8 \times \left(-\frac{8}{x^4}\right)^2$ soi	M1	Must be clearly identified not in expansion
	11.25 or $\frac{45}{4}$	A1	
6(a)(i)	$6 \times 6 \times 5 \times 4 \times 3$ oe	M1	
	2160	A1	
6(a)(ii)	Full correct calculation (360 + 900) ‘how many end with 0’+ ‘how many end with 2, 4, 6’ oe	M2	M1 for any correct product soi Eg $(6 \times 5 \times 4 \times 3 \times 1)$ or 360 $(5 \times 5 \times 4 \times 3 \times 1)$ or 300 $(5 \times 5 \times 4 \times 3 \times 3)$ or 900
	1260 cao	A1	
6(b)	${}^{15}C_7 - {}^9C_7$	M1	
	6399	A1	

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6(c)(i)	$\frac{n!}{(n-3)!3!} + \frac{n!}{(n-2)!2!}$	B2	B1 for either expression correct
	$\frac{n(n-1)(n-2)}{6} + \frac{n(n-1)}{2}$	M2	M1 for either expression correct
	$\frac{n(n-1)(n-2+3)}{6}$ or $\frac{n^3 - 3n^2 + 2n}{6} + \frac{3n^2 - 3n}{6}$ leading to $\frac{1}{6}(n^3 - n)$	A1	
6(c)(ii)	$n(n^2 - 25) = 0$ oe	M1	
	$n = 5$ as the only solution	A1	
7	$\frac{d}{dx}(\sin 3x) = 3 \cos 3x$ soi	B1	
	$u = (1 + \sin 3x)^4$ $\frac{du}{dx} = 4(1 + \sin 3x)^3 (3 \cos 3x)$ soi	M1	FT <i>their</i> $3 \cos 3x$
	$\frac{dy}{dx} = \frac{\sqrt{x}(4(1 + \sin 3x)^3 (3 \cos 3x)) - (1 + \sin 3x)^4 \times \frac{1}{2}x^{-\frac{1}{2}}}{(\sqrt{x})^2}$	M1	FT <i>their</i> $\frac{du}{dx}$ <i>or their</i> $\frac{dv}{dx}$ but not both
	Correct derivative	A1	
	Evaluates <i>their</i> derivative at $x = 1.9$ and multiplies by h	M1	
	$0.651h$	A1	
8(a)	$x = 6\sqrt{3} \sin 60$ $y = -6\sqrt{3} \cos 60$ oe and completion to $9\mathbf{i} - 3\sqrt{3}\mathbf{j}$	B2	B1 for either x or y correct Allow SC1 for verification that $9\mathbf{i} - 3\sqrt{3}\mathbf{j}$ has a bearing of 120° and that $9\mathbf{i} - 3\sqrt{3}\mathbf{j}$ has a magnitude of $6\sqrt{3}$
8(b)	$(5\mathbf{i} + 16\mathbf{j}) + 3(9\mathbf{i} - 3\sqrt{3}\mathbf{j})$ oe, isw	B1	
8(c)	$29\mathbf{i} + 16\mathbf{j} + t(-12\sqrt{3}\mathbf{j})$ oe, isw	B1	

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8(d)	Forms \overline{AB} or \overline{BA} when $t = 1$ e.g. $\overline{BA} = (32\mathbf{i} + (16 - 9\sqrt{3})\mathbf{j}) - (29\mathbf{i} + (16 - 12\sqrt{3})\mathbf{j})$ oe	B1	FT <i>their</i> (b) and (c) with $t = 1$
	$\sqrt{3^2 + (3\sqrt{3})^2}$	M1	FT <i>their</i> \overline{AB} or \overline{BA}
	6 (km)	A1	cao
9(a)	$h = \sqrt{x^2 - \left(\frac{x}{2}\right)^2}$ oe or $\cos 30 = \frac{h}{x}$ oe or $\frac{1}{2}xh = \frac{1}{2}x^2 \sin 60$	M1	Correct expression connecting x and h
	$x = \frac{2h}{\sqrt{3}}$ oe	A1	Must be $x =$
	$V = \frac{1}{2} \times \left(\textit{their} \frac{2h}{\sqrt{3}}\right)^2 \times \sin 60^\circ \times 5$ or $\frac{1}{2} \times h \times \textit{their} \frac{2h}{\sqrt{3}} \times 5$	M1	
	Correct completion to given answer $V = \frac{5\sqrt{3}h^2}{3}$	A1	
9(b)	Correct derivative of V e.g. $\frac{10\sqrt{3}}{3}h$	B1	
	$\frac{dh}{dt} = \frac{dV}{dt} \times \frac{dh}{dV}$ soi	B1	Not $\frac{\partial V}{\partial h}$
	$0.5 \div \left(\frac{10\sqrt{3}}{3} \times 0.1\right)$ oe	M1	
	0.866 (metres per minute) or 0.8660[25...] rot to 4 or more sf	A1	Allow $\frac{\sqrt{3}}{2}$ isw
10(a)	$\ln x - 1$	B2	B1 for $[1 \times] \ln x + x \times \frac{1}{x} [-2]$ oe

Question	Answer	Marks	Partial Marks
10(b)	$x + \frac{1}{x} + 2$	B1	
	$\frac{dy}{dx} = \frac{x^2}{2} + \ln x + 2x (+c)$	M2	M1 for $\frac{dy}{dx} = \dots + \ln x + \dots$ or for $\frac{dy}{dx} = \frac{x^2}{2} + \dots + 2x$
	Substitution to find c : $\frac{e^2}{2} + 2e = \frac{e^2}{2} + \ln e + 2e + c$ [$c = -1$]	M1	FT <i>their</i> attempt to integrate dependent on at least M1
	$y = \int \left(\frac{x^2}{2} + 2x + \ln x - 1 \right) dx$	A1	
	Integrates and uses (a) $y = \frac{x^3}{6} + \frac{2x^2}{2} + x \ln x - 2x + C$	M1	Dependent on M2M1 FT error in c only
	$\frac{e^3}{6} + e^2 = \frac{e^3}{6} + e^2 + e \ln e - 2e + C$	M1	Substitution to find C Dependent on previous M1
	$y = \frac{x^3}{6} + x^2 + x \ln x - 2x + e$	A1	
11	$B\left(\frac{\pi}{10}, 0\right)$ soi	B1	
	$\int_0^{\frac{\pi}{4}} e^{\frac{x}{2}} dx - \int_0^{\frac{\pi}{10}} \cos 5x dx$	M2	M1 Integrates $e^{\frac{x}{2}}$ to $ke^{\frac{x}{2}}$, $k \neq 0$ M1 Integrates $\cos 5x$ to $k \sin 5x$, $k > 0$ or $k = -\frac{1}{5}$
	$\left[2e^{\frac{x}{2}} \right]_0^{\frac{\pi}{4}} - \left[\frac{\sin 5x}{5} \right]_0^{\frac{\pi}{10}}$	A2	A1 for each part correct
	$\left[2e^{\frac{\pi}{8}} - 2e^0 \right] - \left[\frac{1}{5} \sin \frac{5\pi}{10} - \frac{1}{5} \sin 0 \right]$	M1	M1 for correct attempt at subtraction and for one correct use of limits dependent on at least M1 for integration and B1
	$2e^{\frac{\pi}{8}} - \frac{11}{5}$ isw	A1	