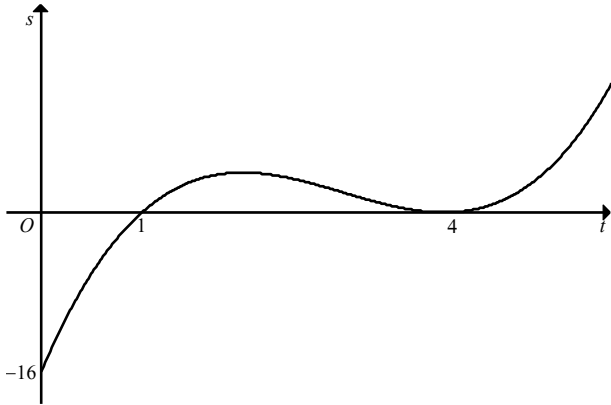
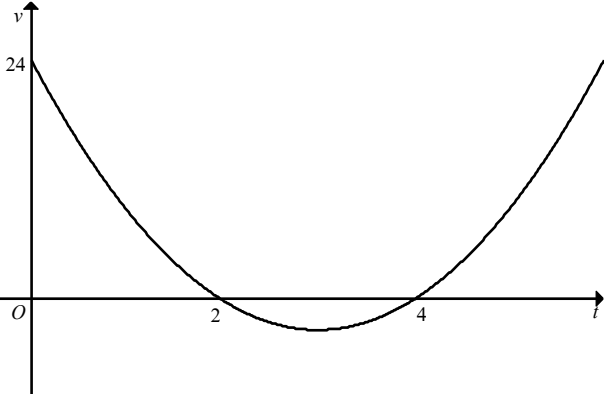
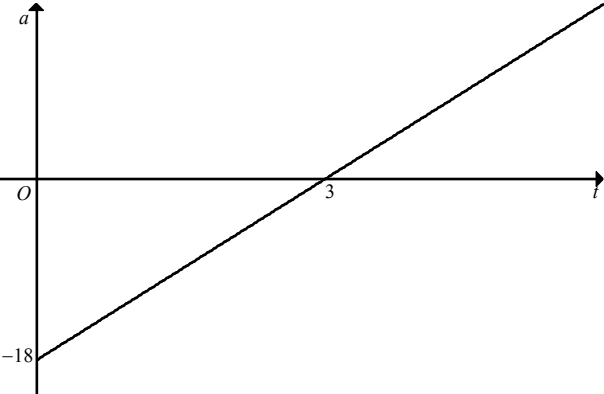


Question	Answer	Marks	Partial marks
1	$5x+2*3$ and $5x+2*-3$ oe	M1	where * could be = or any inequality sign
	Critical values: $\frac{1}{5}, -1$ soi	A2	A1 for one correct value
	$x \leq -1$ $x \geq \frac{1}{5}$ oe mark final answer	A1	
	Alternative method		
	$(5x+2)^2 * 3^2$	(M1)	where * could be = or any inequality sign
	Critical values: $\frac{1}{5}, -1$ soi	(A2)	A1 for $25x^2 + 20x - 5[*0]$
	$x \leq -1$ $x \geq \frac{1}{5}$ oe mark final answer	(A1)	
2 (a)	Fully correct graph with all intercepts stated 	2	B1 for correct cubic shape with maximum in the first quadrant, a point of tangency to the t -axis at the minimum point; must meet the s -axis B1 for correct intercepts; must have attempted the correct shape
2(b)	$v: 2(t-4)(t-1) + (t-4)^2 (1)$ or $s: t^3 - 9t^2 + 24t - 16$ and $v: 3t^2 - 18t + 24$	M1	
	$v: 3(t-4)(t-2)$	A1	

Question	Answer	Marks	Partial marks
2(c)	Fully correct graph with all intercepts stated 	B2	B1 for correct quadratic shape with minimum in the fourth quadrant; must meet the v -axis B1 for correct intercepts; must have attempted the correct shape
2(d)	$6t - 18$ or $3(t - 4) + (3t - 6)$ oe	B1	FT <i>their</i> 3-term quadratic expression oe for v Correct linear expression for a from their v which must be either a 3-term quadratic or an expression that would simplify to a 3-term quadratic
2(e)	Fully correct ruled graph with all intercepts stated 	3	B1 for a single ruled line with positive gradient in fourth and first quadrants; must meet the a -axis and cross the t -axis B1 FT for a line with t -intercept 3 FT <i>their</i> $r(-18) \div$ <i>their</i> 6 providing <i>their</i> a is a linear expression of the form $mt + c$ B1 FT for a line with a -intercept -18 FT <i>their</i> (-18) providing <i>their</i> a is a linear expression of the form $mt + c$

Question	Answer	Marks	Partial marks
3	$\frac{3\sqrt{x+2}}{\sqrt{x+2}+4} = 1$ soi OR $g(x) = f^{-1}(1) \text{ and } f^{-1}(x) = \frac{4x}{3-x} \text{ oe}$	2	M1 for $f(\sqrt{x+2}) [= 1]$ soi or for $g(x) = f^{-1}(1)$ soi
	$x = 2$ nfw	2	M1 FT for correct equation without an algebraic fraction e.g. $\sqrt{x+2} = 2$ FT <i>their</i> $\frac{3\sqrt{x+2}}{\sqrt{x+2}+4} = 1$ providing M1 previously awarded and $fg(x)$ is an algebraic fraction
	Alternative method		
	Solves $\frac{3x}{x+4} = 1$ to find $x = 2$ and states $g(x) = 2$	(2)	M1 for solving $f(x) = 1$ to find $x = k$ and states $g(x) = k$, where k is a constant
$x = 2$ nfw	(2)	M1 FT for $\sqrt{x+2} = k$ FT $g(x) = k$ <i>their</i> providing M1 previously awarded	

Question	Answer	Marks	Partial marks
4(a)	$\left[\frac{dy}{dx} = \right]$ $4(\cos 2x(2 \cos 2x) + \sin 2x(-2 \sin 2x))$ oe	M1	Use of the product rule with correct structure
	$\left[\frac{dy}{dx} = \right] 4(\cos 2x(2 \cos 2x) + \sin 2x(-2 \sin 2x))$ oe, isw	A1	
	$\left[\frac{dy}{dx} \Big _{x=\frac{\pi}{6}} = \right] 4 \left(2 \cos^2 \frac{2\pi}{6} - 2 \sin^2 \frac{2\pi}{6} \right) \text{oe}$	M1	dep on previous M1 FT <i>their</i> $\frac{dy}{dx}$ providing it is of the form $a \cos^2 2x - b \sin^2 2x$ or equivalent where a, b are positive integers
	$\left[\frac{dy}{dx} \Big _{x=\frac{\pi}{6}} = \right] -4$	A1	

Question	Answer	Marks	Partial marks
4(b)	$\left[\text{When } x = \frac{\pi}{6} \right] y = \sqrt{3}$	B1	
	Gradient of normal = $\frac{1}{4}$	M1	FT $\frac{-1}{\text{their } \frac{dy}{dx} \Big _{x=\frac{\pi}{6}}}$ from part (a)
	Equation of normal: $y = \frac{1}{4}x + \sqrt{3} - \frac{\pi}{24}$ or $y = \frac{1}{4}x + c$ and $\sqrt{3} = \frac{1}{4}\left(\frac{\pi}{6}\right) + c$ or $y - \sqrt{3} = \frac{1}{4}\left(x - \frac{\pi}{6}\right)$ oe	M1	FT $\frac{-1}{\text{their } \frac{dy}{dx} \Big _{x=\frac{\pi}{6}}}$ and <i>their y</i> , providing <i>their y</i> $\neq 0$
	$0 - \sqrt{3} = \frac{1}{4}\left(x - \frac{\pi}{6}\right)$	M1	FT <i>their</i> equation of normal providing gradient is $\frac{-1}{\text{their } \frac{dy}{dx} \Big _{x=\frac{\pi}{6}}}$
	$\left(\frac{\pi}{6} - 4\sqrt{3}, 0\right)$ or exact equivalent; mark final answer	A1	dep on all previous marks awarded and a fully correct solution to (a) or a correct derivative and gradient of tangent at $x = \frac{\pi}{6}$ stated in this part
5(a)(i)	300	B1	
5(a)(ii)	252	2	M1 for $21 \times 4 \times 3 \times 1$ oe OR Starts with 5 OR ends with 0: $1 \times 4 \times 3 \times 5$ oe or 60 or Starts with 2, 4, 6 or 8 OR ends with 2, 4, 6 or 8: $4 \times 4 \times 3 \times 4$ oe or 192 OR [All possible –] ends with 5: $4 \times 4 \times 3 \times 1$ oe or 48

Question	Answer	Marks	Partial marks
5(a)(iii)	108	2	<p>M1 for $9 \times 4 \times 3 \times 1$ oe</p> <p>OR</p> <p>Ends with 5: $4 \times 4 \times 3 \times 1$ oe or 48</p> <p>or</p> <p>Ends with 0: $5 \times 4 \times 3 \times 1$ oe or 60</p> <p>OR</p> <p>Starts 5, ends 0: $1 \times 4 \times 3 \times 1$ oe or 12</p> <p>or</p> <p>Does not start 5: $4 \times 4 \times 3 \times 2$ oe or 96</p>
5(b)	<p>Correct simplified equation:</p> $(n+1)^2 = 33 \times 12 \times 11$ oe, nfw	B2	<p>B1 for an equation with simplified algebraic component $(n+1)^2$ oe</p> <p>or simplified numerical component $33 \times 12 \times 11$ oe, nfw</p>
	$n = 65$	B1	dep on B2 ; must be the only solution

Question	Answer	Marks	Partial marks
6	$r = 3\text{nfww}$	B1	stated or very clearly implied
	$2\pi = 4\pi r^2 \times \frac{dr}{dt}$ soi or $\frac{dr}{dt} = \frac{1}{2r^2}$ oe and $\frac{dS}{dr} = 8\pi r$	M1	Uses relevant chain rule e.g. $\frac{dV}{dt} = \frac{dV}{dr} \times \frac{dr}{dt}$ to find the derivatives and values of $\frac{dr}{dt}$ and $\frac{dS}{dr}$
	$\frac{dr}{dt} = \frac{1}{18}$ and $\frac{dS}{dr} = 24\pi$ soi	A1	
	Correct chain rule including $\frac{dS}{dt}$	B1	e.g. $\frac{dS}{dt} = \frac{dS}{dr} \times \frac{dr}{dt}$ or $\frac{dr}{dt} = \frac{dS}{dt} \times \frac{dr}{dS}$ oe
	$\frac{dS}{dt} = \frac{4\pi}{3}$ isw or 4.19 or 4.188 to 4.1888	2	M1 for $\frac{dS}{dt} = 24\pi \times \frac{1}{18}$
	Alternative method 1		
	$r = 3\text{nfww}$	(B1)	stated or very clearly implied
	$\frac{dV}{dr} = 4\pi r^2$ and $\frac{dS}{dr} = 8\pi r$	(M1)	Finds correct expressions for and values of $\frac{dV}{dr}$ and $\frac{dS}{dr}$
	$\frac{dV}{dr} = 36\pi$ and $\frac{dS}{dr} = 24\pi$ soi	(A1)	
	Correct chain rule including $\frac{dS}{dt}$	(B1)	e.g. $\frac{dS}{dt} = \frac{dS}{dr} \times \frac{dr}{dV} \times \frac{dV}{dt}$ or $\frac{dS}{dt} = \frac{dS}{dV} \times \frac{dV}{dt}$
$\frac{dS}{dt} = \frac{4\pi}{3}$ isw or 4.19 or 4.188 to 4.1888	(2)	M1 for $\frac{dS}{dt} = 24\pi \times \frac{1}{36\pi} \times 2\pi$ or $\frac{2}{3} \times 2\pi$	

Question	Answer	Marks	Partial marks
6	Alternative method 2		
	$r = \sqrt[3]{\frac{3V}{4\pi}}$ nfw	(B1)	stated or very clearly implied
	$S = 4\pi \left(\sqrt[3]{\frac{3V}{4\pi}} \right)^2 \rightarrow \frac{dS}{dV} = 4\pi \times \left(\frac{3}{4\pi} \right)^{\frac{2}{3}} \times \frac{2}{3} V^{-\frac{1}{3}}$	(M1)	
	$\frac{dS}{dV} = \frac{2}{3}$ oe soi	(A1)	
	Correct chain rule including $\frac{dS}{dt}$	(B1)	e.g. $\frac{dS}{dt} = \frac{dS}{dV} \times \frac{dV}{dt}$
	$\frac{dS}{dt} = \frac{4\pi}{3}$ isw or 4.19 or 4.188 to 4.1888	(2)	M1 for $\frac{dS}{dt} = \frac{2}{3} \times 2\pi$
	Alternative method 3		
	$r = 3$ nfw	(B1)	stated or very clearly implied
	$r = \sqrt{\frac{S}{4\pi}}, V = \frac{4}{3}\pi \left(\sqrt{\frac{S}{4\pi}} \right)^3, \frac{dV}{dS} = \frac{4}{3}\pi \times \frac{1}{(4\pi)^{\frac{3}{2}}} \times \frac{3}{2} S^{\frac{1}{2}}$	(M1)	
	$S = 36\pi$ and $\frac{dV}{dS} = \frac{3}{2}$ oe soi	(A1)	
	Correct chain rule including $\frac{dS}{dt}$	(B1)	e.g. $\frac{dS}{dt} = \frac{dS}{dV} \times \frac{dV}{dt}$
	$\frac{dS}{dt} = \frac{4\pi}{3}$ isw or 4.19 or 4.188 to 4.1888	(2)	M1 for $\frac{dS}{dt} = \frac{1}{1.5} \times 2\pi$

Question	Answer	Marks	Partial marks
7(a)	Forms a correct equation from which the logarithms can be eliminated : has consistent powers of $\ln x$ in all terms $\frac{n}{2}(12 \ln x + (n-1) \times 4 \ln x) * 43 \times 24 \ln x$ oe, soi OR uses log laws to combine terms $\ln(x^{6n} \times x^{2n(n-1)}) * \ln x^{24 \times 43}$ or better	3	where * is = or any inequality sign M2 for $a = 6$ and $d = 4$ or $a = 6 \ln x$ soi and $d = 4 \ln x$ soi or $a = \ln x^6$ soi and $d = \frac{2}{3} \ln x^6$ soi or $a = \frac{3}{2} \ln x^4$ soi and $d = \ln x^4$ soi or for $\ln x^{12 \times \frac{n}{2}} + \ln x^{4(n-1) \times \frac{n}{2}} * \ln x^{24 \times 43}$ oe or M1 for any correct expression for d or for a correct expression for the sum to n terms using <i>their a</i> and <i>their d</i> providing <i>their d</i> is not one of the given terms
	$2n^2 + 4n - 1032$ [*0] oe	A1	
	Solves <i>their</i> 3-term quadratic in n	M1	dep on attempt at the sum of an AP
	$n = 22$ cao, nfw	A1	dep on all previous marks awarded

Question	Answer	Marks	Partial marks
7(b)	Correct term e.g. $[u_{25} =]$ $6 \ln x + 24 \times 4 \ln x$ or $\ln x^6 + 24 \times \frac{2}{3} \ln x^6$ or $\frac{3}{2} \ln x^4 + 24 \ln x^4$ or $2 \ln x^3 + 24 \times (2 \ln x^7 - 5 \ln x^2)$ oe or $2 \ln x^3 + 24 \times (5 \ln x^2 - 2 \ln x^3)$ oe	B1	
	Forms and correctly simplifies an equation e.g. $102 \ln x = 408$ or $17 \ln x^6 = 408$ or $\frac{51}{2} \ln x^4 = 408$ or $\ln \frac{x^6 \times x^{336}}{x^{240}} = 408$ or $\ln \frac{x^6 \times x^{240}}{x^{144}} = 408$	M1	FT <i>their</i> u_{25} providing it is an expression for the term of an AP which requires the simplification/collection of two natural logarithms
	$x = e^4$	A1	

Question	Answer	Marks	Partial marks
8	For A : $x = \frac{1}{3}$	B1	
	$\frac{dy}{dx} = -\frac{15}{x^2} + \frac{10}{x^3}$ oe. isw OR $\frac{dy}{dx} = \frac{-15x^2 + 10x}{x^4}$ oe, isw	B2	B1 for each correct term OR for $\frac{dy}{dx} = \frac{-15x^2 + \dots}{x^4}$ oe or $\frac{\dots + 10x}{x^4}$
	Solves <i>their</i> $\frac{dy}{dx} = 0$ as far as $x = \dots$	M1	FT <i>their</i> $\frac{dy}{dx}$ providing at least one term is correct
	B : $\left(\frac{2}{3}, \frac{45}{4}\right)$ oe, nfw	A2	A1 for each correct coordinate
	Correct plan e.g. $\int_{\text{their } \frac{1}{3}}^{\text{their } \frac{2}{3}} \left(\frac{15}{x} - \frac{5}{x^2}\right) dx - \frac{1}{2} \times \text{their } \frac{45}{4} \times \left(\text{their } \frac{2}{3} - \text{their } \frac{1}{3}\right)$ or $\int_{\text{their } \frac{1}{3}}^{\text{their } \frac{2}{3}} \left(\frac{15}{x} - \frac{5}{x^2} - \left(\text{their } \frac{135}{4}x - \text{their } \frac{45}{4}\right)\right) dx$	M1	
	$\int \left(\frac{15}{x} - \frac{5}{x^2}\right) dx = 15 \ln x + \frac{5}{x}$ oe	B2	B1 for $15 \ln x$ or $k \ln x + \frac{5}{x}$ oe
	$\left(15 \ln \frac{2}{3} + \frac{15}{2}\right) - \left(15 \ln \frac{1}{3} + 15\right)$ or exact equivalent	M1	FT <i>their</i> $\frac{1}{3}$ and <i>their</i> $\frac{2}{3}$ providing at least B1 awarded for integration
	Area of shaded region: $15 \ln 2 - 9.375$ or $15 \ln 2 - \frac{75}{8}$ or exact equivalent	A1	dep on all previous marks awarded
9(a)	$\tan 3x = \frac{1}{\sqrt{3}}$ or $\frac{\sqrt{3}}{3}$ or 0.57735...	B2	B1 for $\frac{3}{\cos 3x} = \frac{\sqrt{3}}{\sin 3x}$ oe
	$3x = 30$ or 210 or -150 or -330	M1	Finds one correct and valid triple angle May be in radians for this mark implied by one correct value of x
	x : 10, 70, -50, -110 and no extras in range	A2	A1 for any two correct angles ignoring extras

Question	Answer	Marks	Partial marks
9(b)	$\sin\left(y + \frac{\pi}{3}\right) = 0$	B1	
	$\cos\left(y + \frac{\pi}{3}\right) = \frac{1}{2}$	B1	
	$y + \frac{\pi}{3} = 0$ or π or 2π or $\frac{\pi}{3}$ or $\frac{5\pi}{3}$	M1	Finds one correct and valid compound angle May be in degrees for this mark
	$y: \frac{2\pi}{3}, \frac{5\pi}{3}, 0, \frac{4\pi}{3}$ oe, nfww	A2	A1 for any two correct angles ignoring extras
10	$n = 6$ stated; nfww	B2	B1 for first term: $(3x^2)^n$ or $(3x^2)^6$ soi
	$-6(3x^2)^5 a + 2(729x^{10}) = 972x^{10}$ oe and $\frac{6 \times 5(3x^2)^4 (-a)^2}{2} + 6(3x^2)^5 \times \frac{2}{x^2}(-a) + 729x^8 = bx^8$ oe	B3	B2 for one correct equation OR B1 for second term: $n(-a)(3x^2)^{n-1}$ or $6(-a)(3x^2)^5$ or $-1458ax^{10}$ soi B1 for third term: $\frac{n(n-1)(-a)^2(3x^2)^{n-2}}{2}$ or $\frac{6(5)(-a)^2(3x^2)^4}{2}$ or $1215a^2 x^8$ soi B1 for $1 \quad [+]$ $\frac{2}{x^2}$ $[+]$ $\frac{1}{x^4}$ soi
	$a = \frac{1}{3}$	B2	B1 for $-1458a + 1458 = 972$ soi
	$b = -108$	B2	B1 for $1215a^2 - 2916a + 729$ soi