

Question	Answer	Marks	Partial Marks
1(a)	[Distance between centres =] $\sqrt{(15-3)^2 + (-4-2)^2}$ oe	M1	
	$29 - 17 < 13[.41\dots] < 29 + 17$ oe	A1	
1(b)	$y - 17 = 2(x + 5)$ oe	B2	B1 for gradient $\frac{17 - (-0.6)}{-5 + 13.8}$ oe, soi or for $600 + 30x - 8y - 6x + 9 - 4y + 4 = 17^2$ oe
2(a)	[When $x^4 = 0$] $\lg y = 4$	B2	B1 for $\frac{7-5}{6-2}$ oe and correct use of a point and <i>their</i> $\frac{1}{2}$ to find the intercept of the straight line
2(b)	$\lg y = \frac{1}{2}x^4 + 4$ soi	B1	FT <i>their</i> $\frac{1}{2}$ and <i>their</i> 4
	$y = 10^{\frac{1}{2}x^4 + 4}$	M1	FT <i>their</i> $\frac{1}{2}$ and <i>their</i> 4
	$A = 10^4$ or 10000, $b = 10$, $C = \frac{1}{2}$	A1	May be embedded
3	$12(8) + a(4) - 12(2) + b = 0$ oe	B1	
	$12(-1) + a[1] - 12(-1) + b = -15$ oe	B1	
	Correct method of solution	M1	FT <i>their</i> pair of linear equations in a and b
	$a = -19$, $b = 4$	A2	A1 for either correct
	$12x^2 + 5x - 2$	M2	M1 for quadratic factor with 2 correct terms
	$(4x - 1)$ and $(3x + 2)$	A1	
4(a)	100	3	M2 for a fully correct method e.g. [starts 2 and ends 4] $1 \times 5 \times 4 \times 1$ or 20 [starts 1, 3 and ends 2, 4] $2 \times 5 \times 4 \times 2$ or 80 OR [ends 4 and starts 1, 2, 3] $3 \times 5 \times 4 \times 1$ or 60 [ends 2 and starts 1, 3] $2 \times 5 \times 4 \times 1$ or 40 or M1 for a partially correct method equivalent to one of the above statements

Question	Answer	Marks	Partial Marks
4(b)	260	3	<p>M2 for a fully correct method e.g. [starts 4 and ends 2, 3, 5, 7] $1 \times 5 \times 4 \times 4$ or 80 [starts 2, 3, 5 and ends 7 or any two of 2, 3, 5] $3 \times 5 \times 4 \times 3$ or 180</p> <p>OR</p> <p>[ends 7 and starts 2, 3, 4, 5] $4 \times 5 \times 4 \times 1$ or 80 [ends 2, 3, 5 and starts 4 or any two of 2, 3, 5] $3 \times 5 \times 4 \times 3$ or 180</p> <p>or M1 for a partially correct method equivalent to one of the above statements</p>
5	$128 + 448ax + 672a^2x^2 + 560a^3x^3$ soi or $448a = b$ $672a^2 = c$ $560a^3 = -15\,120$ soi	M3	<p>M2 for any 3 correct terms or 2 correct equations</p> <p>or</p> <p>M1 for any 2 correct terms or 1 correct equation or for correct but insufficiently simplified expansion e.g. $2^7 + 7(2^6)(ax) + \frac{7 \times 6}{2}(2^5)(ax)^2 + \frac{7 \times 6 \times 5}{3 \times 2}(2^4)(ax)^3$</p>
	$a = -3$	A1	
	$b = -1344$	A1	FT $448 \times$ <i>their a</i> , providing at least M1 awarded
	$c = 6048$	A1	FT $672 \times$ (<i>their a</i>) ² , providing at least M1 awarded
6(a)	$V = 2x^3 - 195x^2 + 4500x$	B3	B2 for an otherwise correct expression with at most one error or B1 for $(75 - 2x)(60 - x)x$ soi
6(b)	$\left[\frac{dV}{dx} = \right] 6x^2 - 390x + 4500$	B1	FT <i>their</i> integer values of a , b and c
	Equates <i>their</i> $\frac{dV}{dx}$ to 0 and solves for x	M1	FT <i>their</i> values of a , b and c
	$x = 15$ as the only solution	A1	

Question	Answer	Marks	Partial Marks
7(a)	$\frac{\cos x(1 + \sin x) + \cos x(1 - \sin x)}{1 - \sin^2 x}$	M1	
	$\frac{\cos x + \cos x \sin x + \cos x - \cos x \sin x}{1 - \sin^2 x}$ or $\frac{\cos x(1 + \sin x) + \cos x(1 - \sin x)}{\cos^2 x}$	A1	
	$\frac{2 \cos x}{1 - \sin^2 x}$ or $\frac{1 + \sin x + 1 - \sin x}{\cos x}$ or $\frac{2 \cos x}{\cos^2 x}$	A1	
	Completion to the given answer: $\frac{2}{\cos x} = 2 \sec x$ oe	A1	must be fully justified and with all previous steps correct
7(b)(i)	$\tan x = \frac{5}{4}$	M1	
	51.3 or 51.34[0...] rot to 2 or more decimal places -128.7 or -128.65[98...] rot to 2 or more decimal places	A2	and no extras in range A1 for either correct, ignoring extras
7(b)(ii)	$10(1 - \cos^2 2x) - 9 = 3 \cos 2x$	M1	
	$10 \cos^2 2x + 3 \cos 2x - 1 [= 0]$	A1	
	$(5 \cos 2x - 1)(2 \cos 2x + 1) [= 0]$	M1	FT <i>their</i> 3-term quadratic in solvable form
	$\frac{\pi}{3}, \frac{2\pi}{3}$ 0.685 or 0.6847[19...] rot to 4 or more significant figures, 2.46 or 2.456[87...] rot to 4 or more significant figures	A2	and no extras in range A1 for one correct, ignoring extras
8(a)(i)	Valid supported explanation: The function is one-one on this domain with support e.g. [it is quadratic and] the turning point is at $x = -1$	B2	B1 for a correct but incomplete statement e.g. The function is one-one on this domain or [it is quadratic and] the turning point is at $x = -1$

Question	Answer	Marks	Partial Marks
8(a)(ii)	$x^2 + 2x + 5 - y = 0$ or $y = (x + 1)^2 + 4$	M1	
	$x = \frac{-2 \pm \sqrt{2^2 - 4(1)(5 - y)}}{2}$ oe, soi or $x = -1 \pm \sqrt{y - 4}$	A1	
	Justifies the choice of square root	B1	
	$f^{-1}(x) = -1 + \sqrt{x - 4}$	A1	
8(b)(i)	Valid supported explanation: The range of f is a subset of the domain of g with support e.g. $f \geq 5$ oe	B2	B1 for a correct but incomplete statement e.g. The range of f is a subset of the domain of g or $f \geq 5$ oe
8(b)(ii)	$\frac{5(x^2 + 2x + 5)}{x^2 + 2x + 5 + 2} = 4$ oe	M1	
	$x^2 + 2x - 3 [= 0]$	A1	
	$(x - 1)(x + 3) [= 0]$	M1	FT <i>their</i> 3-term quadratic in solvable form
	$x = 1$ as the only solution	A1	
9(a)	first term = $3(1.25)^{19}$ and an attempt at S_{12}	M1	
	Correct sum $S_{12} = \frac{208.166... (1 - 1.25^{12})}{1 - 1.25}$ oe	M2	M1 FT <i>their</i> first term for $S_{12} = \frac{\text{their } 208.166... (1 - 1.25^{12})}{1 - 1.25}$
	11 284	A1	
	Alternative $S_{19} = \frac{3(1 - 1.25^{19})}{1 - 1.25}$ and $S_{31} = \frac{3(1 - 1.25^{31})}{1 - 1.25}$ oe	(B2)	B1 for $S_{19} = \frac{3(1 - 1.25^{19})}{1 - 1.25}$ or $S_{31} = \frac{3(1 - 1.25^{31})}{1 - 1.25}$ oe
	Correct plan: $S_{31} - S_{19}$ oe attempted	(M1)	
	11 284	(A1)	

Question	Answer	Marks	Partial Marks
9(b)	$S_{5n} = \frac{5n}{2} \{2(5) + (5n - 1)(3)\}$ and $S_n = \frac{n}{2} \{2(5) + (n - 1)(3)\}$	B2	B1 for either sum correct
	Forms a correct equation: $\frac{5n}{2} \{2(5) + (5n - 1)(3)\} = \frac{23n}{2} \{2(5) + (n - 1)(3)\}$ oe	M1	FT <i>their</i> sums providing at least B1 awarded
	$n = 21$	A1	
10(a)(i)	Straight line starting at $\left(\frac{\pi}{2}, 1\right)$ and ending at $(\pi, 0)$	B1	
10(a)(ii)	[Distance $\frac{\pi}{2}$ to π : $\frac{1}{2} \times \frac{\pi}{2} [\times 1] = \frac{\pi}{4}$	B1	
	$\left[2 \tan \frac{t}{2} - t\right]_0^{\frac{\pi}{2}}$	M2	M1 for $k \tan \frac{t}{2}$ soi
	$2 \tan \frac{1}{2} \left(\frac{\pi}{2}\right) - \frac{\pi}{2} [-0]$	M1	dep on at least M1 earned
	$2 - \frac{\pi}{4}$ or 1.21 or 1.214[60...] rot to 4 or more significant figures	A1	
10(b)(i)	$v = -e^{2t} + 3e^{-2t}$	B1	
	$3 - (e^{2t})^2 = 0$ or $3 - e^{4t} = 0$ oe	M1	FT <i>their</i> v providing it is of the form $me^{2t} + ne^{-2t}$, where m and n are constants
	$2t = \ln \sqrt{3}$ or $4t = \ln 3$ oe	M1	dep on previous M1 ; FT <i>their</i> 3 which must be > 0
	$t = 0.2747$ cao; nfw	A1	
10(b)(ii)	$\frac{4 - e^{2(\text{their } 0.2747)} - 3e^{-2(\text{their } 0.2747)}}{2} +$ $\left(\frac{4 - e^{2(\text{their } 0.2747)} - 3e^{-2(\text{their } 0.2747)}}{2} - \frac{4 - e^{2(0.5)} - 3e^{-2(0.5)}}{2}\right)$ soi	M2	FT <i>their</i> $t \neq 0$ M1 for $\frac{4 - e^{2(\text{their } 0.2747)} - 3e^{-2(\text{their } 0.2747)}}{2}$ or 0.268 or 0.2679[49...] rot to 4 or more decimal places
	0.447 or 0.4468[58...] rot to 4 or more decimal places	A1	