



0580/22

February/March 2020

1 3.56 5 $\sqrt{196}$ 8 $\sqrt{7}$ 12
K

From the list, write down a number that is

(a) a multiple of 3,

..... 12 [1]

(b) a cube number,

..... 8 [1]

(c) a prime number,

..... 5 [1]

(d) an irrational number.

..... $\sqrt{7}$ [1]

2 The number of people swimming in a pool is recorded each day for 12 days.

K
24 28 13 38 15 26
45 21 48 36 18 38

(a) Complete the stem-and-leaf diagram.

1	3 5 8
2	1 4 6 8
3	6 8 8
4	5 8

Key: 1|3 represents 13 swimmers

[2]

(b) Find the median number of swimmers.

$$\frac{26 + 28}{2}$$

..... 27 [1]

- 3 Point A has coordinates $(6, 4)$ and point B has coordinates $(2, 7)$.

\mathcal{R} Write \vec{AB} as a column vector.

$$\begin{pmatrix} 2 - 6 \\ 7 - 4 \end{pmatrix}$$

$$\vec{AB} = \begin{pmatrix} -4 \\ 3 \end{pmatrix} \quad [1]$$

- 4 Find the interior angle of a regular polygon with 24 sides.

$$\frac{(24 - 2) 180^\circ}{24}$$

$$\dots\dots\dots 165^\circ \dots\dots\dots [2]$$

- 5 Without using a calculator, work out $\frac{15}{28} \div \frac{4}{7}$.

\mathcal{R} You must show all your working and give your answer as a fraction in its simplest form.

$$\frac{15}{28} \times \frac{7}{4} = \frac{15}{4 \times 4} = \frac{15}{16}$$

$$\dots\dots\dots \frac{15}{16} \dots\dots\dots [3]$$

- 6 The table shows the marks scored by 40 students in a test.

R

Mark	5	6	7	8	9	10
Frequency	8	5	11	7	5	4

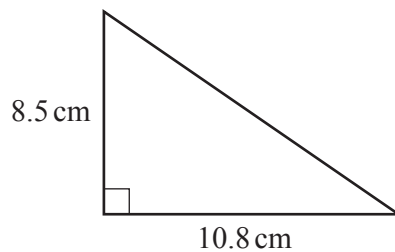
Calculate the mean mark.

$$\frac{5 \times 8 + 6 \times 5 + 7 \times 11 + 8 \times 7 + 9 \times 5 + 10 \times 4}{40}$$

..... 7.2 [3]

7

R



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The diagram shows a right-angled triangle.

- (a) Calculate the area.

$$\frac{1}{2} \times 8.5 \times 10.8$$

..... 45.9 cm² [2]

- (b) Calculate the perimeter.

$$\begin{aligned} \text{hypotenuse} &= \sqrt{8.5^2 + 10.8^2} = 13.744 \\ \text{perimeter} &= 8.5 + 10.8 + 13.744 \end{aligned}$$

..... 33.0 cm [3]

- 8 Calculate the value of $(2.3 \times 10^{-3}) + (6.8 \times 10^{-4})$.

R

Give your answer in standard form.

$$\begin{aligned} &2.3 \times 10^{-3} + 6.8 \times 10^{-4} \\ &= 2.98 \times 10^{-3} \end{aligned}$$

..... 2.98×10^{-3} [1]

- 9 (a) Factorise completely.

\mathcal{R}

$$3x^2 - 12xy$$

$$\underline{3x(x - 4y)} \quad [2]$$

- (b) Expand and simplify.

$$(m-3)(m+2)$$

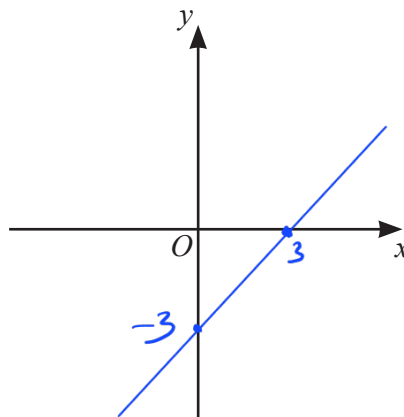
$$m^2 - 3m + 2m - 6$$

$$\underline{m^2 - m - 6} \quad [2]$$

- 10 Sketch the graph of each function.

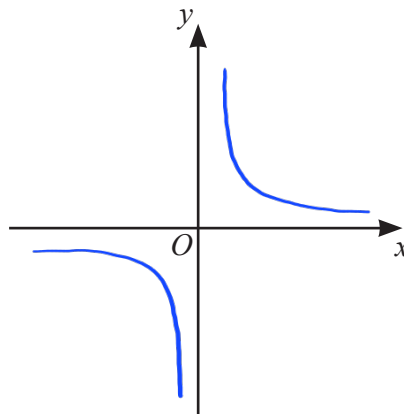
\mathcal{R}

(a) $y = x - 3$

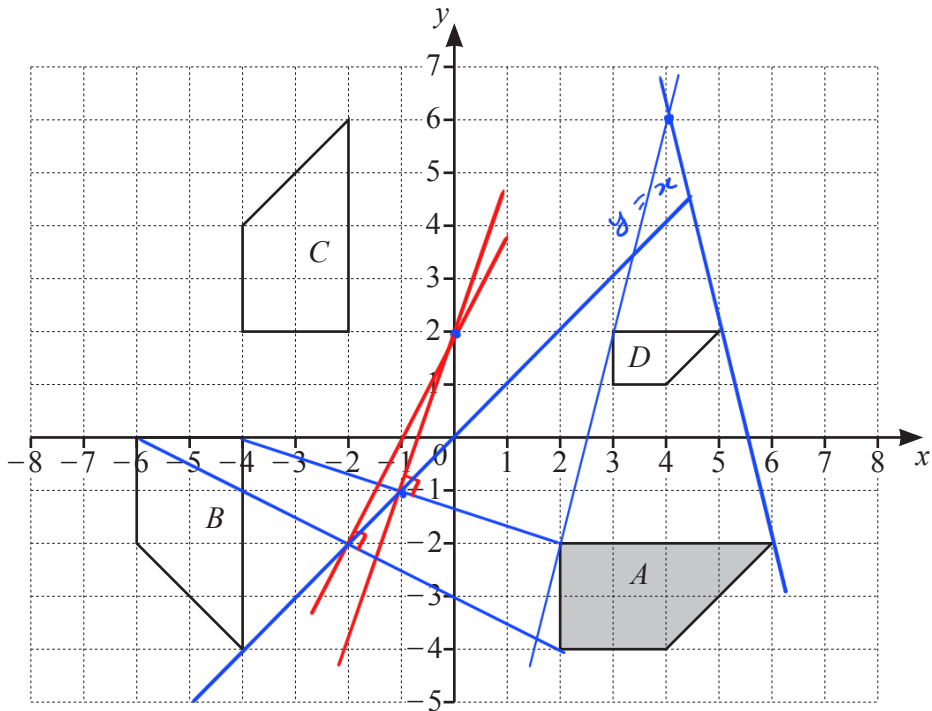


[1]

(b) $y = \frac{1}{x}$



[2]



Describe fully the **single** transformation that maps

- (a) shape *A* onto shape *B*,

Rotation, center $(0, 2)$, clockwise 90°

[3]

- (b) shape *A* onto shape *C*,

Reflection over $y = x$

[2]

- (c) shape *A* onto shape *D*.

Enlargement, center $(4, 6)$, scale factor $\frac{1}{2}$

[3]

- 12 The population of a town decreases exponentially at a rate of 1.7% per year.
 The population now is 250 000.
 Calculate the population at the end of 5 years.
 Give your answer correct to the nearest hundred.

$$250\,000 \left(1 - \frac{1.7}{100}\right)^5 = 229\,460$$

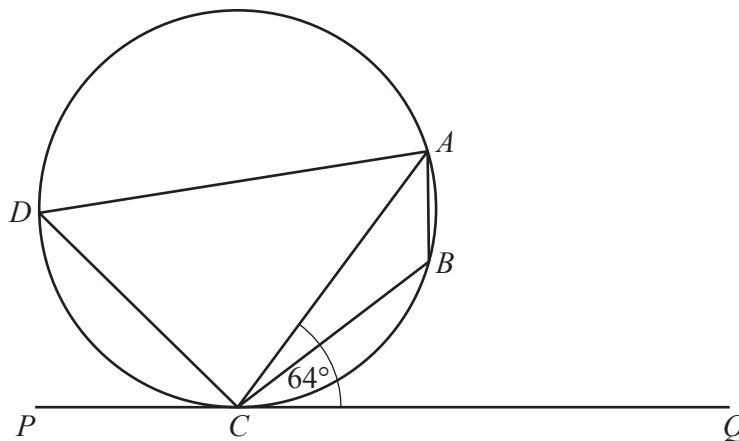
..... 229 500 [3]

- 13 Write the recurring decimal $0.2\dot{6}$ as a fraction.
 You must show all your working.

$$\begin{aligned} x &= 0.2666\dots \\ 10x &= 2.666\dots \\ 100x &= 26.666\dots \\ 90x &= 26 - 2 = 24 \\ x &= \frac{24}{90} \end{aligned}$$

..... $\frac{24}{90}$ [2]

15



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A, B, C and D lie on the circle.
 PCQ is a tangent to the circle at C .
 Angle $ACQ = 64^\circ$.

Work out angle ABC , giving reasons for your answer.

Angle $ABC = 116^\circ$ because $\widehat{ADC} = \widehat{ACQ}$ (alternate segment theorem) and $\widehat{ABC} = 180^\circ - \widehat{ADC} = 180^\circ - 64^\circ = 116^\circ$
 (2 opposite angles in a cyclic quadrilateral add up to 180°) [3]

16 Solve the simultaneous equations.

R You must show all your working.

$$x = 7 - 3y$$

$$x^2 - y^2 = 39$$

$$(7 - 3y)^2 - y^2 = 39$$

$$49 - 2 \times 7 \times 3y + 9y^2 - y^2 = 39$$

$$8y^2 - 42y + 10 = 0$$

$$2(4y - 1)(y - 5) = 0$$

$$y = 0.25 \text{ or } y = 5$$

$$\text{When } y = 0.25, \quad x = 7 - 3 \times 0.25 = 6.25$$

$$\text{When } y = 5, \quad x = 7 - 3 \times 5 = -8$$

$$x = \dots 6.25 \dots \quad y = \dots 0.25 \dots$$

$$x = \dots -8 \dots \quad y = \dots 5 \dots \quad [6]$$

17 A is the point $(3, 5)$ and B is the point $(1, -7)$.

R Find the equation of the line perpendicular to AB that passes through the point A .

Give your answer in the form $y = mx + c$. l

$$m_{AB} = \frac{-7 - 5}{1 - 3} = 6$$

$$m_l = -1 : 6 = \frac{-1}{6}$$

$$\text{Equation of line } l: \quad y - 5 = \frac{-1}{6}(x - 3)$$

$$y = \dots \frac{-1}{6}x + \frac{11}{2} \dots \quad [4]$$

18 A car travels at a constant speed.

R It travels a distance of 146.2 m, correct to 1 decimal place.

This takes 7 seconds, correct to the nearest second.

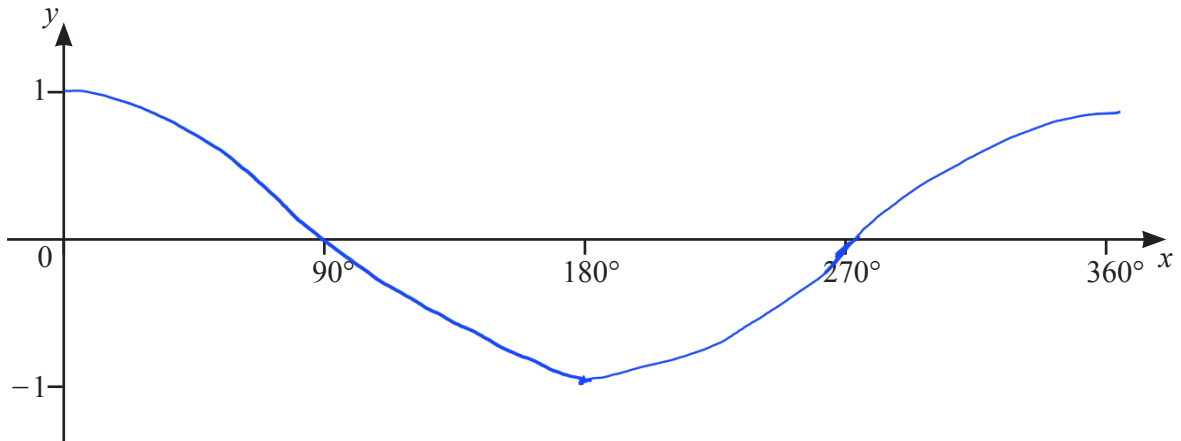
Calculate the upper bound for the speed of the car.

$$\text{speed} = \frac{\text{distance (max)}}{\text{time (min)}} = \frac{146.2 + \frac{0.1}{2}}{7 - \frac{1}{2}} = 22.5$$

$$\dots 22.5 \dots \text{ m/s } [3]$$

19

R



- (a) On the diagram, sketch the graph of $y = \cos x$ for $0^\circ \leq x \leq 360^\circ$. [2]
 (b) Solve the equation $4 \cos x + 2 = 3$ for $0^\circ \leq x \leq 360^\circ$.

$$4 \cos x = 1$$

$$\cos x = 0.25$$

$$x = 75.5^\circ \quad \text{or} \quad x = -75.5^\circ$$

$$\text{or} \quad x = -75.5^\circ + 360^\circ = 284.5^\circ$$

$x = \dots 75.5^\circ \dots$ and $x = \dots 284.5^\circ \dots$ [3]

20

$$x^2 - 12x + a = (x + b)^2$$

R

Find the value of a and the value of b .

$$x^2 - 12x + a = x^2 + 2xb + b^2$$

$$\begin{cases} -12 = 2b \\ a = b^2 \end{cases}$$

$$\begin{cases} b = -6 \\ a = 36 \end{cases}$$

$a = \dots 36 \dots$

$b = \dots -6 \dots$ [2]

21 $\vec{XY} = 3\mathbf{a} + 2\mathbf{b}$ and $\vec{ZY} = 6\mathbf{a} + 4\mathbf{b}$.

$$\vec{ZY} = 2\vec{XY}$$

R

Write down two statements about the relationship between the points X , Y and Z .

1 X, Y, Z are collinear

2 X is the midpoint of YZ [2]