

(a) Draw the image of shape  $A$  after a translation by the vector  $\begin{pmatrix} 8 \\ -6 \end{pmatrix}$ . [2]

(b) Draw the image of shape  $A$  after a reflection in the line  $y = -1$ . [2]

(c) Describe fully the **single** transformation that maps shape  $A$  onto shape  $B$ .

..... [3]

(d) Describe fully the **single** transformation that maps shape  $A$  onto shape  $C$ .

..... [3]

2 (a) A plane has 14 First Class seats, 70 Premium seats and 168 Economy seats.



Find the ratio First Class seats : Premium seats : Economy seats.  
Give your answer in its simplest form.

..... : ..... : ..... [2]

(b) (i) For a morning flight, the costs of tickets are in the ratio

$$\text{First Class : Premium : Economy} = 14 : 6 : 5.$$

The cost of a Premium ticket is \$114.

Calculate the cost of a First Class ticket and the cost of an Economy ticket.

First Class \$ .....

Economy \$ ..... [3]

(ii) For an afternoon flight, the cost of a Premium ticket is reduced from \$114 to \$96.90 .

Calculate the percentage reduction in the cost of a ticket.

..... % [2]

(c) When the local time in Athens is 09 00, the local time in Berlin is 08 00.

A plane leaves Athens at 13 15.

It arrives in Berlin at 15 05 local time.

(i) Find the flight time from Athens to Berlin.

..... h ..... min [1]

(ii) The distance the plane flies from Athens to Berlin is 1802 km.

Calculate the average speed of the plane.

Give your answer in kilometres per hour.

..... km/h [2]

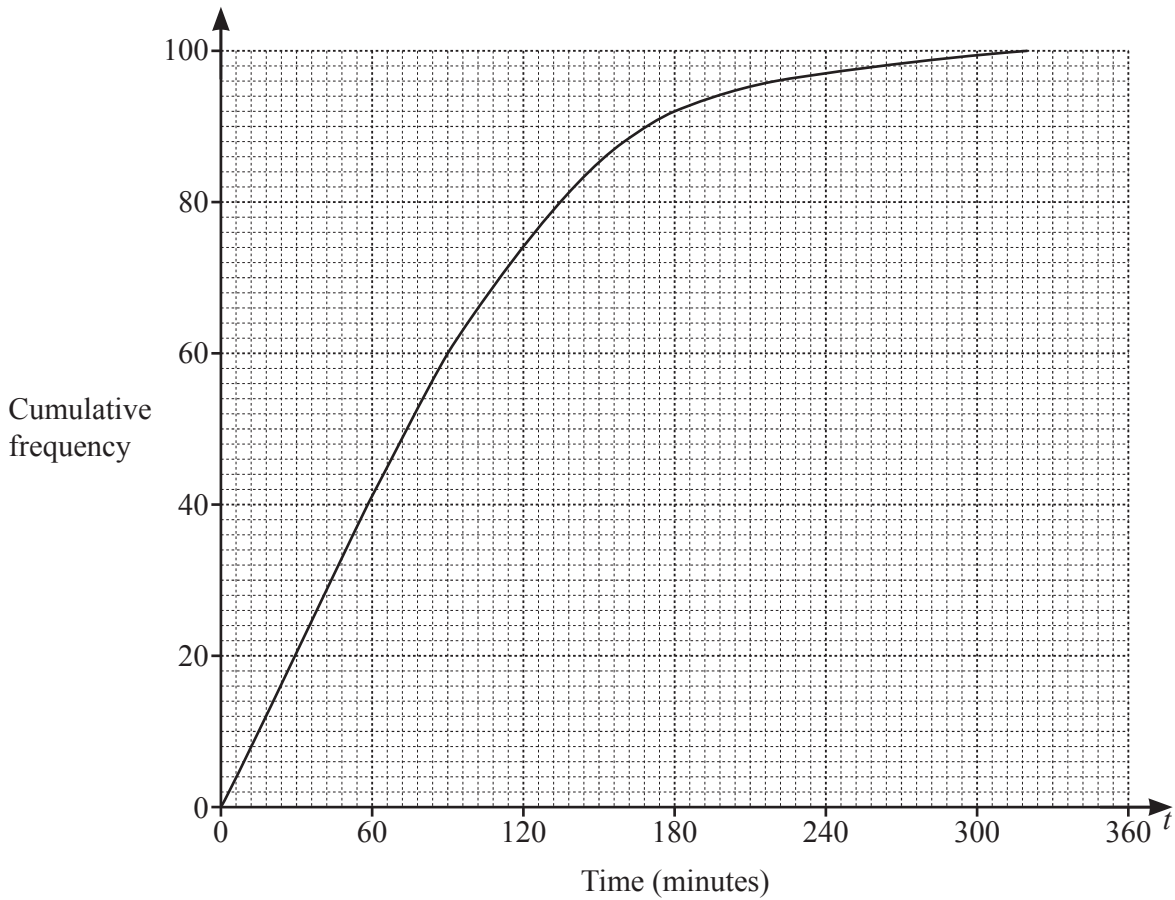
(b) The frequency table shows the times,  $t$  minutes, each of 100 children spent exercising in one week.

Time ( $t$ minutes)	$0 < t \leq 60$	$60 < t \leq 100$	$100 < t \leq 160$	$160 < t \leq 220$	$220 < t \leq 320$
Frequency	41	24	23	8	4

(i) Calculate an estimate of the mean time.

..... min [4]

(ii) The information in the frequency table is shown in this cumulative frequency diagram.



Use the cumulative frequency diagram to find an estimate of

(a) the 60th percentile,

..... min [1]

(b) the number of children who spent more than 3 hours exercising.

..... [2]

(iii) A histogram is drawn to show the information in the frequency table. The height of the bar for the interval  $60 < t \leq 100$  is 10.8 cm.

Calculate the height of the bar for the interval  $160 < t \leq 220$ .

..... cm [2]

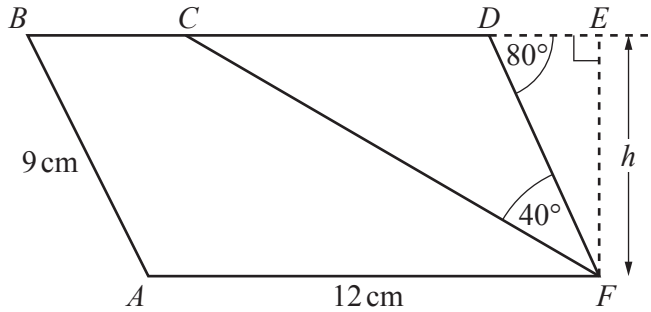
- 4 (a) A rectangle measures 8.5 cm by 10.7 cm, both correct to 1 decimal place.



Calculate the upper bound of the perimeter of the rectangle.

..... cm [3]

- (b)



NOT TO SCALE

*ABDF* is a parallelogram and *BCDE* is a straight line.  
*AF* = 12 cm, *AB* = 9 cm, angle *CFD* = 40° and angle *FDE* = 80°.

- (i) Calculate the height, *h*, of the parallelogram.

*h* = ..... cm [2]

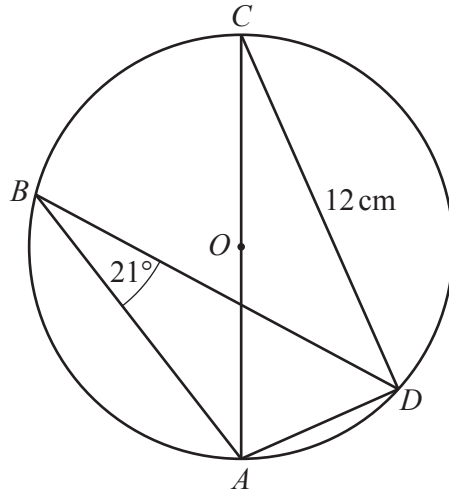
- (ii) Explain why triangle *CDF* is isosceles.

.....  
 ..... [2]

- (iii) Calculate the area of the **trapezium** *ABCF*.

..... cm<sup>2</sup> [3]

(c)



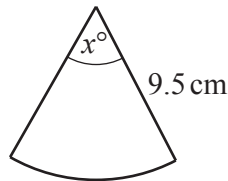
NOT TO SCALE

$A, B, C$  and  $D$  are points on the circle, centre  $O$ .  
Angle  $ABD = 21^\circ$  and  $CD = 12$  cm.

Calculate the area of the circle.

.....  $\text{cm}^2$  [5]

(d)



NOT TO SCALE

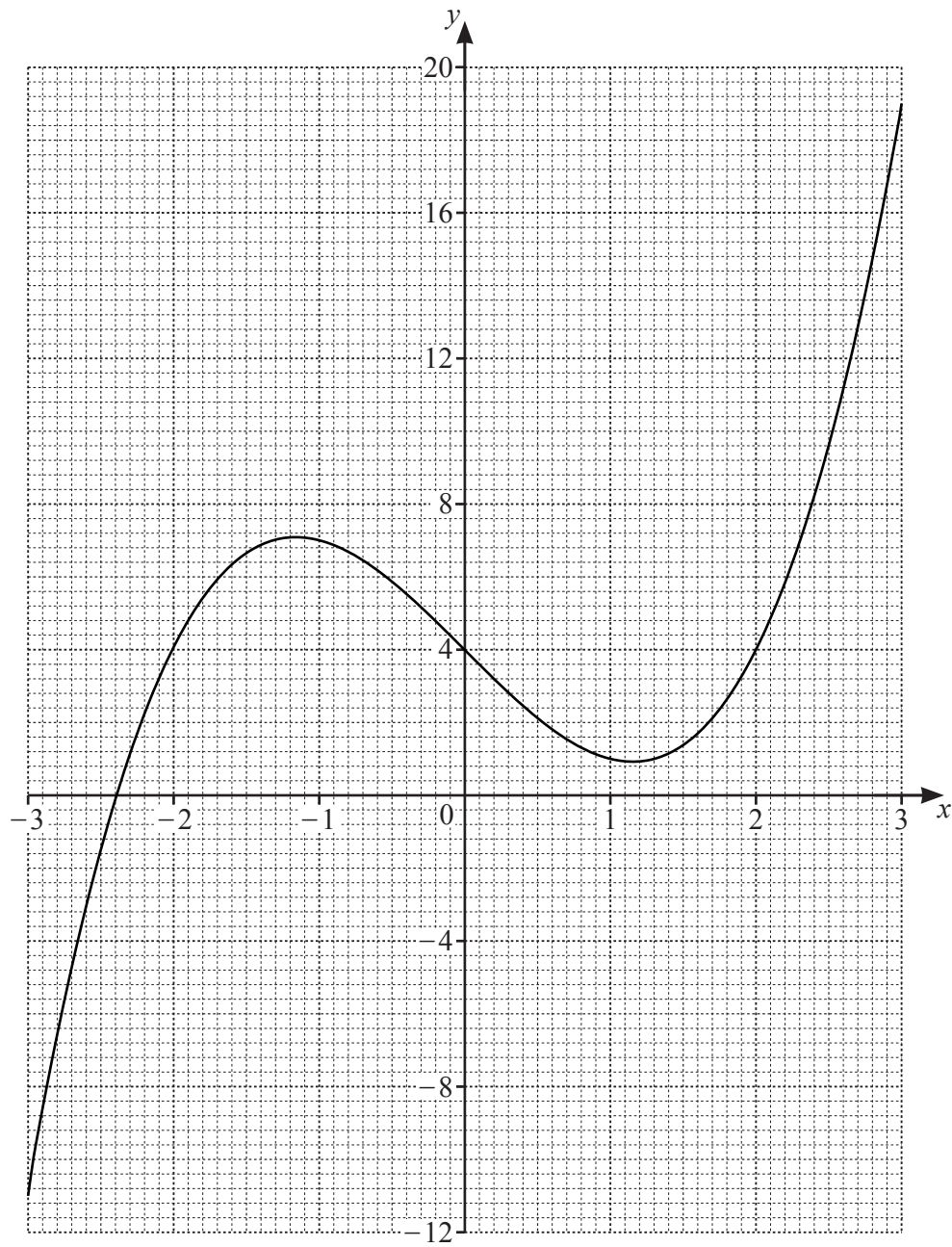
The diagram shows a square with side length 8 cm and a sector of a circle with radius 9.5 cm and sector angle  $x^\circ$ .

The perimeter of the square is equal to the perimeter of the sector.

Calculate the value of  $x$ .

$x =$  ..... [3]

- 5 (a) The diagram shows the graph of  $y = f(x)$  for  $-3 \leq x \leq 3$ .



- (i) Solve  $f(x) = 14$ .

$x = \dots\dots\dots$  [1]

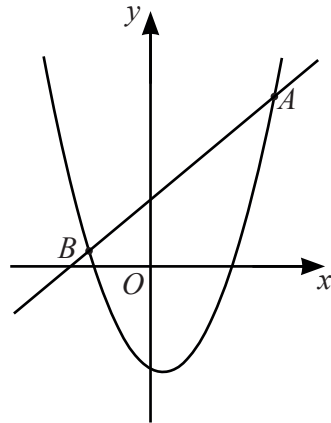
- (ii) By drawing a suitable tangent, find an estimate of the gradient of the graph at the point  $(-2, 4)$ .

$\dots\dots\dots$  [3]

(iii) By drawing a suitable straight line on the grid, solve  $f(x) = 2x - 2$  for  $-3 \leq x \leq 3$ .

$x = \dots\dots\dots$  [3]

(b)



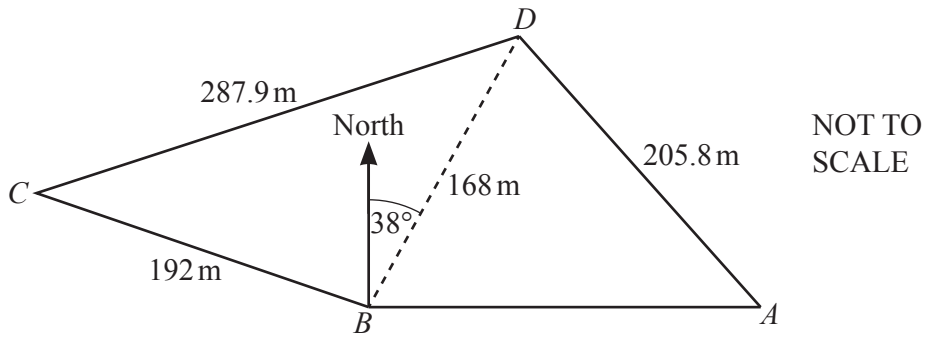
NOT TO SCALE

The diagram shows a curve with equation  $y = 2x^2 - 2x - 7$ .  
 The straight line with equation  $y = 3x + 5$  intersects the curve at the points  $A$  and  $B$ .

Find the coordinates of the points  $A$  and  $B$ .

$A$  (..... , .....)

$B$  (..... , .....) [5]



The diagram shows a field,  $ABCD$ , on horizontal ground.  
 $BC = 192$  m,  $CD = 287.9$  m,  $BD = 168$  m and  $AD = 205.8$  m.

(a) (i) Calculate angle  $CBD$  and show that it rounds to  $106.0^\circ$ , correct to 1 decimal place.

[4]

(ii) The bearing of  $D$  from  $B$  is  $038^\circ$ .

Find the bearing of  $C$  from  $B$ .

..... [1]

(iii)  $A$  is **due east** of  $B$ .

Calculate the bearing of  $D$  from  $A$ .

..... [5]

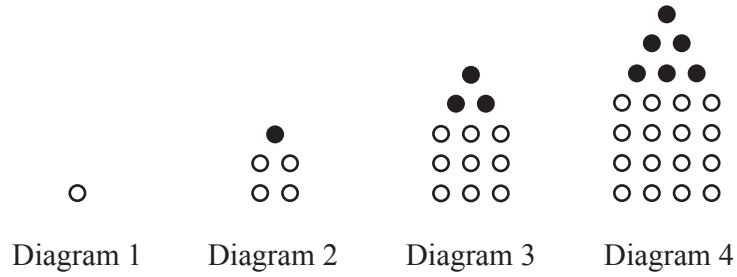
(b) (i) Calculate the area of triangle  $BCD$ .

.....  $\text{m}^2$  [2]

(ii) Tomas buys the triangular part of the field,  $BCD$ .  
The cost is \$35 750 per hectare.

Calculate the amount he pays.  
Give your answer correct to the nearest \$100.  
[1 hectare = 10 000  $\text{m}^2$ ]

\$ ..... [2]



These are the first four diagrams of a sequence.  
 The diagrams are made from white dots and black dots.

(a) Complete the table for Diagram 5 and Diagram 6.

Diagram	1	2	3	4	5	6
Number of white dots	1	4	9	16		
Number of black dots	0	1	3	6		
Total number of dots	1	5	12	22		

[2]

(b) Write an expression, in terms of  $n$ , for the number of white dots in Diagram  $n$ .

..... [1]

(c) The expression for the total number of dots in Diagram  $n$  is  $\frac{1}{2}(3n^2 - n)$ .

(i) Find the total number of dots in Diagram 8.

..... [1]

(ii) Find an expression for the number of black dots in Diagram  $n$ .  
 Give your answer in its simplest form.

..... [2]

(d)  $T$  is the total number of dots used to make **all** of the first  $n$  diagrams.

$$T = an^3 + bn^2$$

Find the value of  $a$  and the value of  $b$ .  
You must show all your working.

$$a = \dots\dots\dots$$

$$b = \dots\dots\dots [5]$$

8 (a) Factorise completely.



$$3a^2b - ab^2$$

..... [2]

(b) Solve the inequality.

$$3x + 12 < 5x - 3$$

..... [2]

(c) Simplify.

$$(3x^2y^4)^3$$

..... [2]

(d) Solve.

$$\frac{2}{x} = \frac{6}{2-x}$$

$x =$  ..... [3]

(e) Expand and simplify.

$$(x-2)(x+5)(2x-1)$$

..... [3]

(f) Alan invests \$200 at a rate of  $r\%$  per year compound interest. After 2 years the value of his investment is \$206.46 .

(i) Show that  $r^2 + 200r - 323 = 0$ .

[3]

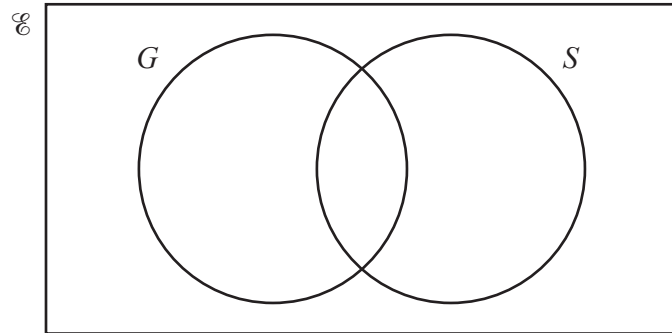
(ii) Solve the equation  $r^2 + 200r - 323 = 0$  to find the rate of interest. Show all your working and give your answer correct to 2 decimal places.

$r = \dots\dots\dots$  [3]

9 (a) There are 32 students in a class.



5 do not study any languages.  
 15 study German ( $G$ ).  
 18 study Spanish ( $S$ ).



(i) Complete the Venn diagram to show this information. [2]

(ii) A student is chosen at random.

Find the probability that the student studies Spanish but not German.

..... [1]

(iii) A student who studies German is chosen at random.

Find the probability that this student also studies Spanish.

..... [1]

- (b) A bag contains 54 red marbles and some blue marbles.  
36% of the marbles in the bag are red.

Find the number of blue marbles in the bag.

..... [2]

- (c) Another bag contains 15 red beads and 10 yellow beads.  
Ariana picks a bead at random, records its colour and replaces it in the bag.  
She then picks another bead at random.

- (i) Find the probability that she picks two red beads.

..... [2]

- (ii) Find the probability that she does not pick two red beads.

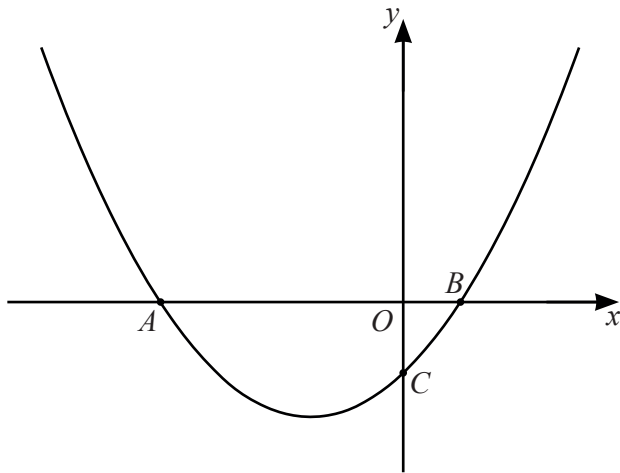
..... [1]

- (d) A box contains 15 red pencils, 8 yellow pencils and 2 green pencils.  
Two pencils are picked at random without replacement.

Find the probability that at least one pencil is red.

..... [3]

10 (a)



NOT TO SCALE

The diagram shows a sketch of the curve  $y = x^2 + 3x - 4$ .

(i) Find the coordinates of the points  $A$ ,  $B$  and  $C$ .

$A$  (....., .....) )

$B$  (....., .....) )

$C$  (....., .....) [4]

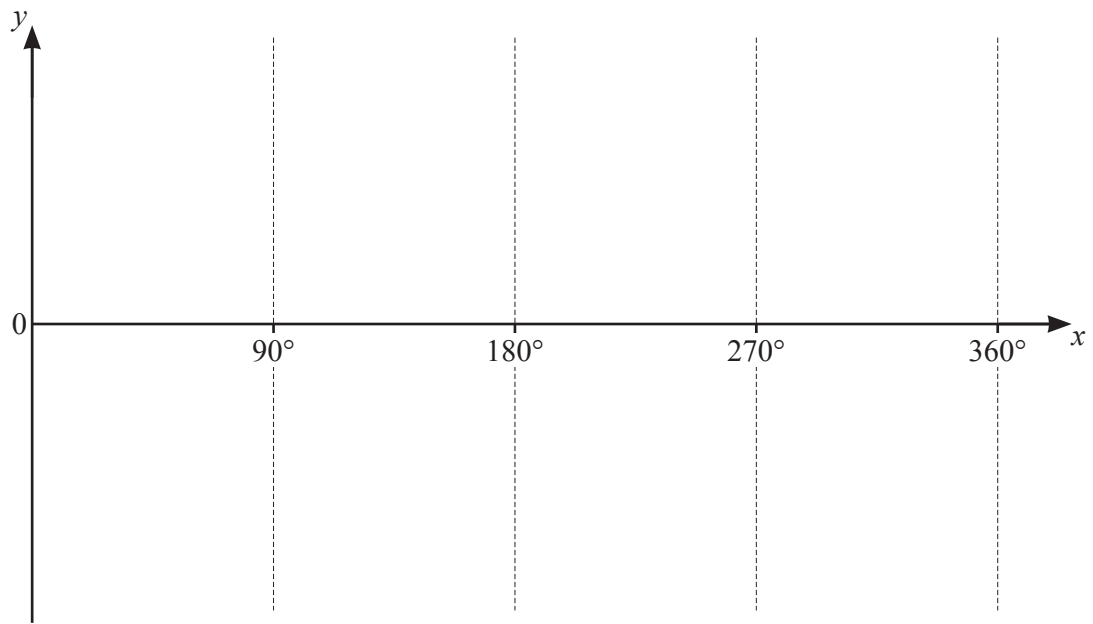
(ii) Differentiate  $x^2 + 3x - 4$ .

..... [2]

(iii) Find the equation of the tangent to the curve at the point  $(2, 6)$ .

..... [3]

(b)



(i) On the diagram, sketch the graph of  $y = \tan x$  for  $0^\circ \leq x \leq 360^\circ$ . [2]

(ii) Solve the equation  $5 \tan x = -7$  for  $0^\circ \leq x \leq 360^\circ$ .

$x = \dots\dots\dots$  or  $x = \dots\dots\dots$  [3]